

Chapter 1

BASIC ALGEBRAIC OPERATIONS

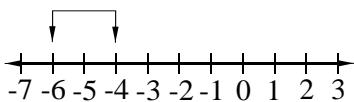
1.1 Numbers

1. The numbers -3 and 14 are integers. They are also rational numbers since they can be written

as $\frac{-3}{1}$ and $\frac{14}{1}$.

2. The absolute value of -6 and 6 and the absolute value of -7 is 7 . We write these as $|-6| = 6$ and $|-7| = 7$.

3. $-6 < -4$; -6 is to the left of -4



4. The reciprocal of $\frac{3}{2}$ is $\frac{1}{\frac{3}{2}} = 1 \left(\frac{2}{3} \right) = \frac{2}{3}$.

5. 3 : integer, rational $\left(\frac{3}{1}\right)$, real

$\sqrt{-4}$: imaginary

$-\frac{\pi}{6}$: irrational, real

$\frac{1}{8}$: rational, real

6. $-\sqrt{-6}$: imaginary

$-2.33 = -\frac{233}{100}$: rational, real

$\frac{\sqrt{7}}{3}$: irrational

-6 : integer, rational, real

7. $|3| = 3$, $|-4| = 4$, $\left| -\frac{\pi}{2} \right| = \frac{\pi}{2}$

$\sqrt{-1}$ is imaginary and the absolute value will be considered in Chapter 12.

8. $|-0.857| = 0.857$, $|\sqrt{2}| = \sqrt{2}$, $\left| -\frac{19}{4} \right| = \frac{19}{4}$

$\frac{\sqrt{-5}}{-2}$ is imaginary and the absolute value will be considered in Chapter 12.

9. $6 < 8$

10. $7 > 5$

11. $-\pi > -3.1416$

12. $-4 < 0$

13. $-|-3| = -3 \Rightarrow -4 < -3 = -|-3|$

14. $-\sqrt{2} > -1.42$ 15. $-\frac{1}{3} > -\frac{1}{2}$ 16. $-0.6 < 0.2$

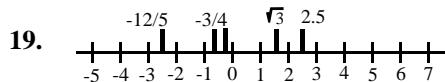
17. The reciprocal of $3 = \frac{1}{3}$. The reciprocal of $-\frac{4}{\sqrt{3}}$ is $-\frac{1}{\frac{4}{\sqrt{3}}} = -\frac{\sqrt{3}}{4}$.

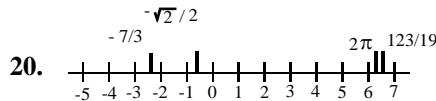
The reciprocal of $\frac{y}{b}$ is $\frac{1}{\frac{y}{b}} = \frac{b}{y}$.

18. The reciprocal of $-\frac{1}{3}$ is $-\frac{1}{-\frac{1}{3}} = 3$.

The reciprocal of 0.25 is $\frac{1}{0.25} = 4$.

The reciprocal of $2x$ is $\frac{1}{2x}$.





21. An absolute value is not always positive, $|0| = 0$ which is not positive.

22. Since $-2.17 = \frac{-217}{100}$ it is rational.

23. The reciprocal of the reciprocal of any positive or negative number is the number itself. ($n \neq 0$)

$$\frac{1}{\frac{1}{n}} = 1 \times \frac{n}{1} = n.$$

24. $-\frac{10}{11} = -0.909090\dots = -0.\overline{90}$ is a rational number between -0.9 and -1.0 since $-0.9 < -0.\overline{90} < -1.0$.

25. Since $0.13 = \frac{13}{100} \cdot \frac{\frac{3}{13}}{\frac{3}{13}} = \frac{3}{\frac{300}{13}} = \frac{3}{23.0769} \dots < \frac{3}{23} = \frac{3}{23} \cdot \frac{\frac{14}{3}}{\frac{14}{3}} = \frac{14}{107.3} < \frac{14}{100} = 0.14$
 $\frac{3}{23}$ is a rational number between 0.13 and 0.14 with numerator 3 and an integer, 23, in the denominator.

26. Yes, $|b-a| = |b|-|a|$ as shown below.

$$a > 0 \Rightarrow |a| = a$$

$$b > a \text{ and } a > 0 \Rightarrow b > 0 \Rightarrow |b| = b$$

$$b > a \Rightarrow b-a > 0 \Rightarrow |b-a| = b-a$$

$$|b-a| = b-a = |b|-|a|$$

27. $\frac{-3.1 \quad -3 \quad -1 \quad \sqrt{5} \quad \pi \quad |-8|}{-3.1 \quad -|-3| \quad -1 \quad 2.236 \quad 3.14 \quad 8 \quad 9}$

28. $-|-6|, -4, -\sqrt{10}, \frac{1}{5}, 0.25, |\pi|$

29. (a) $b-a$; $b > a$, positive integer
(b) $a-b$; $b > a$, negative integer

- (c) $\frac{b-a}{b+a}$, positive rational number less than 1

30. (a) $a+b$ positive integer

- (b) $\frac{a}{b}$, positive rational integer

- (c) $a \times b$, positive integer

31. (a) Let x be a positive integer, then $|x| = x$ which is positive integer and thus an integer. Yes. Let x be a negative integer, then $|x| = -x$ which is a positive integer and thus an integer. Yes.

- (b) Let x be a positive or negative integer, then the reciprocal is $\frac{1}{x}$ which is the ratio of two integers, 1 and x , and is thus a rational number. Yes.

32. (a) Yes, $|\text{positive or negative rational}| = \text{positive rational}$

- (b) Yes, $\frac{\text{integer}}{\text{integer}}$ has reciprocal $\frac{\text{integer}}{\text{integer}}$ which is rational

33. (a) x is a positive number located to the right of 0.

- (b) x is a negative number located to the left of -4 .

34. (a) $|x| < 1$ describes

$$\begin{array}{ccccccc} & & & \textcircled{1} & & & \\ \text{---} & & & & & & \text{---} \\ & & & -1 & & & 1 \\ & & & & & & \end{array}$$

$$\Leftrightarrow -1 < x < 1$$

- (b) $|x| > 2$ describes

$$\begin{array}{ccccccc} & & & \textcircled{2} & & & \\ \text{---} & & & & & & \text{---} \\ & & & -2 & & & 2 \\ & & & & & & \end{array}$$

$$\Leftrightarrow x < -2 \text{ or } x > 2$$

35. If $x > 1$, then $\frac{1}{x}$ is a positive number less than 1.
(x is between 0 and 1)

36. For $x < 0$, $|x| > 0$

37. $a + bj = a + b\sqrt{-1}$ which for $b = 0$ is $a + bj = a$, a real number. The complex number $a + bj$ is a real number for all values of a and $b = 0$.

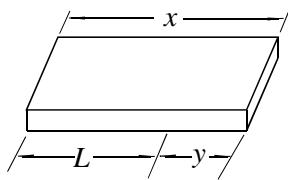
38. variables: w, t constants: 0.1, 1, c

$$\begin{aligned} 39. \frac{1}{C_r} &= \frac{1}{C_1} + \frac{1}{C_2} = \frac{1}{0.0040} + \frac{1}{0.0010} \\ &= \frac{0.0010 + 0.0040}{(0.0040)(0.0010)} \\ C_r &= \frac{(0.0040)(0.0010)}{0.0010 + 0.0040} = 0.0008 \text{ F} \end{aligned}$$

40. $|100 \text{ V}| = 100 \text{ V}, | -200 \text{ V}| = 200 \text{ V}$
 -200 V has the greater absolute value.

$$\begin{aligned} 41. N &= \frac{a \text{ bits}}{\text{byte}} \cdot \frac{1000 \text{ bytes}}{\text{kilobytes}} \cdot n \text{ kilobytes} \\ &= 1000 an \text{ bits} \end{aligned}$$

42.

 x = length of base in ft $12x$ = length of base in inches $y + L = 12x$, all dimensions in inches

$$L = 12x - y$$

43. Yes, this statement is correct since -20 is larger than -30 .

44. For $I < 4A$, $R > 12 \Omega$ (ohms)

1.2 Fundamental Operations of Algebra

1. $16 - 2 \times (-3) = 16 - (-6) = 22$

2. $\frac{-18}{-6} + 5 - (-3) = 3 + 5 - (-6) = 8 - (-6) = 14$

3. $\frac{-12}{8-2} + \frac{5-1}{2(-1)} = \frac{-12}{6} + \frac{4}{-2} = -2 + (-2) = -4$

4. $\frac{7 \times 6}{0 \times 6} = \frac{42}{0}$ is undefined

5. $8 + (-4) = 8 - 4 = 4$

6. $-4 + (-7) = -11$

7. $-3 + 9 = -(3 - 9) = -(-6) = 6$

8. $18 - 21 = -3$ 9. $-19 - (-16) = -19 + 16 = -3$

10. $8 - (-10) = 8 + 10 = 18$

11. $8(-3) = -(8 \times 3) = -24$ 12. $-9(3) = -27$

13. $-7(-5) = 35$

14. $\frac{-9}{3} = -3$

15. $\frac{-6(20-10)}{-3} = \frac{-6(10)}{-3} = \frac{-60}{-3} = 20$

16. $\frac{-28}{-7(5-6)} = \frac{-28}{-7(-1)} = \frac{-28}{7} = -4$

17. $-2(4)(-5) = (-8)(-5) = 40$

18. $-3(-4)(-6) = 12(-6) = -72$

19. $2(2-7) \div 10 = 2(-5) \div 10 = -10 \div 10 = -1$

20. $\frac{-64}{-2|4-8|} = \frac{-64}{-2|-4|} = \frac{-64}{(-2)(4)} = \frac{-64}{-8} = 8$

21. $-9 - |2-10| = -9 - 1| -8 | = -9 - 8 = -17$

22. $(7-7) \div (5-7) = 0 \div (-2) = 0$

23. $\frac{17-7}{7-7} = \frac{10}{0}$ is undefined

24. $\frac{(7-7)(2)}{(7-7)(-1)} = \frac{0}{0}$ is indeterminate

25. $8 - 3(-4) = 8 - (-12) = 8 + 12 = 20$

26. $-20 + 8 \div 4 = -20 + 2 = -18$

27. $-2(-6) + \left| \frac{8}{-2} \right| = 12 + |-4| = 12 + 4 = 16$

28. $\frac{|-2|}{-2} - (-2)(-5) = \frac{2}{-2} - 10 = -1 - 10 = -11$

29. $30(-6)(-2) \div (0 - 40) = 360 \div (-40) = -9$

30. $\frac{7 - |-5|}{-1(-2)} = \frac{7 - 5}{2} = \frac{2}{2} = 1$

31. $\frac{24}{3+(-5)} - 4(-9) \div 3 = 24 - 36 \div -3 = 2 - 12 - (12) = -24$

32. $\frac{-18}{3} - \frac{-|-6|}{-1} = -6 - \frac{4-6}{-1} = -6 - 2 = -8$

33. $-7 - \frac{|-14|}{2(2-3)} - 3|6-8| = -7 - \frac{14}{2(-1)} - 3|-2| = -7 - \frac{14}{-2} - 3(2) = -7 - (-7) - 6 = 0 - 6 = -6$

34. $-7(-3) + \frac{-6}{-3} - |-9| = 21 + (2) - 9 = 23 - 9 = 14$

35. $\frac{3|(-9)-2(-3)|}{1+(-10)} = \frac{3|-9+6|}{-9} = \frac{3|-3|}{-9} = \frac{3(3)}{-9} = -1$

36. $\frac{20(-12)-40(-15)}{98-|-98|} = \frac{-240-(-600)}{98-98} = \frac{360}{0}$ is undefined

37. $6(7) = 7(6)$ demonstrates the commutative law of multiplication.

38. $6+8=8+6=6$ demonstrates the commutative law of addition.

39. $6(3+1) = 6(3) + 6(1)$ demonstrates the distributive law.

40. $4(5 \times \pi) = (4 \times 5)(\pi)$ demonstrates the associative law of multiplication.

41. $3+(5+9)=(3+5)+9$ demonstrates the associative law of addition.

42. $8(3-2)=8(3)-8(2)$ demonstrates the distributive law.

43. $(\sqrt{5} \times 3) \times 9 = \sqrt{5} \times (3 \times 9)$ demonstrates the associative law of multiplication.

44. $(3 \times 6) \times 7 = 7 \times (3 \times 6)$ demonstrates the commutative law of multiplication.

45. $-a + (-b) = -a - b$ which is expression (d).

46. $b - (-a) = b + a = a + b$, expression (a).

47. $-b - (-a) = -b + (a) = -b + a = a - b$ expression (b).

48. $-a - (-b) = -a + b = b - a$, expression (c).

49. $|5 - (-2)| = |-5 - | - 2 ||$

50. $|-3 - |-7|| > |1 - 3| - 7|$

51. (a) The product of an even number of negative numbers is positive.

(b) The product of an odd number of negative numbers is negative.

52. Subtraction is *not* commutative. $7 - 5 \neq 5 - 7$: counterexample.

53. The definition $|x| = \begin{cases} x, & \text{if } x \geq 0 \\ -x, & \text{if } x < 0 \end{cases}$

is correct because it is equivalent to the definition on page 3 where $|x|$ is defined as x , the number itself for $x = 0$ or $x > 0$ (positive) and $|x|$ is the corresponding positive number ($= -x$) for $x < 0$ (negative).

54. The expression was evaluated as

$$\begin{aligned} 24 - 6 \div 2 \cdot 3 &= 18 \div 2 \cdot 3 \\ &= 9 \cdot 3 \\ &= 27, \end{aligned}$$

the error was doing the subtraction before the division and multiplication in violation of the order of operations. The correct order of operations is,

$$\begin{aligned} 24 - 6 \div 2 \cdot 3 &= 24 - 3 \cdot 3 \\ &= 24 - 9 \\ &= 15 \end{aligned}$$

55. (a) $-xy = 1 \Rightarrow y = -\frac{1}{x}$ which shows the numbers are negative reciprocals.

(b) $\frac{x-y}{x-y} = 1$ provided $x \neq y$ (to prevent division by zero). The numbers cannot be equal.

56. (a) Consider $x, y \geq 0 \Rightarrow x + y \geq 0 \Rightarrow |x| = x, |y| = y, |x+y| = x+y \Rightarrow |x+y| = |x|+|y|$ holds for $x, y \geq 0$.

Now consider

$x, y < 0 \Rightarrow x + y < 0 \Rightarrow |x| = -x, |y| = -y, |x+y| = -(x+y) = -x + (-y) = |x|+|y| \Rightarrow |x+y| = |x|+|y|$ holds for $x, y < 0$.

In other words, if one or both is zero, or they have the same sign, the equality $|x+y| = |x|+|y|$ holds.

Now suppose one, say $x > 0$, and the other, $y < 0$. $x > 0 \Rightarrow |x| = x, y < 0 \Rightarrow |y| = -y$ while $x+y$ could be (i) positive and (ii) negative.

(i) $x+y > 0 \Rightarrow |x+y| = x+y \neq x-y = |x|+|y|$, so the equality $|x+y| = |x|+|y|$ does not hold.

(ii) $x+y < 0 \Rightarrow |x+y| = -(x+y) = -x-y \neq x-y = |x|+|y|$, so the equality $|x+y| = |x|+|y|$ does not hold.

Summary: $|x+y| = |x|+|y|$ holds when x and y have the same sign, or one or both is zero.

(b) An argument similar to (a) shows x and y must have opposite signs, or one or both is zero.

57. $10 - (-15) = 10 + 15 = 25$

58. $-86 - (-1396) = 1310$

59. $2.1 - 1.5(3) = -2.4 \text{ kW}\cdot\text{h}$

60. Since batting average = $\frac{\# \text{ of hits}}{\# \text{ of times at bat}}$ = $\frac{0}{0}$ before the season starts, the batting average is indeterminate.

61. $\frac{-7 + (-3) + (2) + (3) + (1) + (-4) + (-6)}{7} = -2^\circ\text{C}$

62. $(20)(5) + (-5)(25) = 100 + (-125)$
 $= -25 \text{ m below flare gun}$

63. Sum of voltages = $(6) + (-2) + (8) + (-5) + (3)$
 $= 4 + 8 + (-5) + 3$
 $= 12 + (-5) + 3$
 $= 7 + 3$
 $= 10 \text{ V}$

64. (a) Change = 2nd reading - 1st reading
 $= -2 - 7 = -9 \text{ lb/in.}^2$

(b) Change = 2nd reading - 1st reading
 $= -9 - (-2) = -7 \text{ lb/in.}^2$

(c) Change = 2nd reading - 1st reading
 $= -6 - (-9) = 3 \text{ lb/in.}^2$

65. $100 \text{ m} + 200 \text{ m} = 200 \text{ m} + 100 \text{ m}$ illustrates the commutative law of addition.

66. Tank 1: total amount leaked = $\frac{12 \text{ gal}}{\text{h}} \cdot 7\text{h} = 84 \text{ gal}$

Tank 2: $\frac{7 \text{ gal}}{\text{h}} \cdot 12\text{h} = 84 \text{ gal}$

The commutative property of multiplication is the fundamental law of algebra illustrated.

- 67.** Total time spent browsing = time spent browsing first site + time spent browsing second site

$$= 4 \text{ persons} \cdot \frac{8 \text{ min}}{\text{person}} + 4 \text{ persons} \cdot \frac{6 \text{ min}}{\text{person}}$$

$$= 4(8+6) \text{ min}$$

= 56 min which illustrates the distributive law

- 68.** Distance = rate \times time

$$= (600+50) \times 3$$

= $600 \times 3 + 50 \times 3$, distributive law

$$= 1950 \text{ km}$$

1.3 Calculators and Approximate Numbers

1. Yes, 0.390 has three significant digits since the 0 after the 9 is not needed to locate the decimal.
2. 35.303 rounded to four significant digits is 35.30.
3. In finding the product of the approximate numbers 2.483 and 30.5 on a calculator the display shows 75.7315 which rounds to 75.7 since 30.5 has three significant digits.
4. $38.3 - 21.9(-3.58) = 116.702$ using exact numbers.
Estimating $40 - 20(-4) = 40 + 80 = 120$.
5. 8 cylinders is exact because they can be counted.
55 mi/h is approximate since it is measured.
6. 0.002 mm, approximate; \$7.50, exact
7. 24 and 1440 are exact.
8. 50 keys, exact; 50 h, approximate
9. 1 cm and 9 g are approximate

- 10.** 90, 75, 15 are exact.

- 11.** 107 has 3 significant digits. 3004 has 4 significant digits. 1040 has 3 significant digits.

- 12.** 3600 has 2 significant digits
730 has 2 significant digits
2055 has 4 significant digits

- 13.** 6.80 has 3 significant digits; the zero indicates precision.
6.08 has 3 significant digits; the zero is not used for decimal location, and is not a place-holder only.
0.068 has 2 significant digits.

- 14.** 0.8730 has 3 significant digits
0.0075 has 2 significant digits
0.0305 has 3 significant digits

- 15.** 3000 has 1 significant digit. 3000.1 has 5 significant digits. 3000.10 has 6 significant digits.

- 16.** 1.00 has 3 significant digits
0.01 has 1 significant digits
0.0100 has 4 significant digits

- 17.** (a) 0.01 is more precise (more decimal places).
(b) 30.8 is more accurate (more significant digits).

- 18.** (a) 0.041 and 7.673 have the same precision
(b) 7.673 is more accurate than 0.041

- 19.** (a) Both numbers have the same precision with digits in the tenths place.
(b) 78.0 with 3 significant digits is more accurate than 0.1 with 1 significant digit.

- 20.** (a) 0.004 is more precise than 7040
(b) 7040 is more accurate than 0.004

- 21.** (a) 0.004 is more precise (more decimal places).
 (b) Both have the same accuracy

- 22.** (a) 50.060 and $| -8.914 |$ have the same precision
 (b) 50.060 is more accurate than $| -8.914 |$

- 23.** (a) $4.936 = 4.94$ rounded to 3 significant digits.
 (b) $4.936 = 4.9$ rounded to 2 significant digits.

- 24.** (a) 3 significant digits: $80.53 \rightarrow 80.5$
 (b) 2 significant digits: $80.53 \rightarrow 81$

- 25.** (a) $-50.893 = -50.9$ (3 significant digits)
 (b) $-50.893 = -51.0$ (2 significant digits)

- 26.** (a) $7.004 = 7.00$ to 3 significant digits
 (b) $7.004 = 7.0$ to 2 significant digits

- 27.** (a) $9549 = 9550$ rounded to 3 significant digits.
 (b) $9549 = 9500$ rounded to 2 significant digits.

- 28.** (a) 3 significant digits: $30.96 \rightarrow 31.0$
 (b) 2 significant digits: $30.96 \rightarrow 31$

- 29.** (a) $0.9449 = 0.945$ (3 significant digits)
 (b) $0.9949 = 0.94$ (2 significant digits)

- 30.** (a) 3 significant digits: $0.9999 \rightarrow 1.00$
 (b) 2 significant digits: $0.9999 \rightarrow 1.0$

- 31.** (a) Estimate: $13 + 1 - 2 = 12$
 (b) Calculator: $12.78 + 1.0495 - 1.633 = 12.1965$
 $= 12.20$

- 32.** (a) Estimate: $4 \times 17 = 68$
 (b) Calculator: $3.64 \times 17.06 = 62.0984 = 62.1$

- 33.** (a) Estimate: $1 \times 4 - 9 = -5$
 (b) Calculator: $0.6572 \times 3.94 - 8.651 = -5.99$

- 34.** (a) Estimate: $40 - 30 \div 4 = 32.5$
 (b) Calculator: $41.5 - 26.4 \div 3.7 = 34.3$

35. (a) Estimate: $0.04 - \frac{0.05}{2} = 0.015$

(b) Calculator: $0.0350 - \frac{0.0450}{1.909} = 0.0114$

36. (a) Estimate: $\frac{0.3}{1 \times 0.5} = 0.6$

(b) Calculator: $\frac{0.3275}{1.096 \times 0.50085} = 0.5966134943$
 $= 0.5966$

37. (a) Estimate: $\frac{20 \times 0.02}{10 - 8} = 0.2$

(b) Calculator: $\frac{23.962 \times 0.01537}{10.965 - 8.249} = 0.1356$

38. (a) Estimate: $\frac{0.7 + 0.05}{300 \times 3} = 0.00083\dots$

(b) Calculator: $\frac{0.69378 + 0.04997}{257.4 \times 3.216} = 0.0008984675496$
 $= 0.0008985$

39. (a) Estimate: $\frac{4000}{500} - \frac{2 \times 300}{400} = 6.5$

(b) Calculator: $\frac{3872}{503.1} - \frac{2.056 \times 309.6}{395.2} = 6.085610980$
 $= 6.086$

40. (a) Estimate: $\frac{1}{0.6} - \frac{4}{1-3} = 3\bar{6}$

(b) Calculator: $\frac{1}{0.5926} - \frac{3.6957}{1.054 - 2.935} = 3.652231698$
 $= 3.6522$

- 41.** $0.9788 + 14.9 = 15.8788$ since 4 is the number of decimal places in the least precise number.

42. $17.311 - 22.98 = -5.669$

- 43.** $-3.142(65) = -204.2$ (The product has the accuracy of the approximate number).

44. $8.62 \div 1728 = 0.00499$

45. 2.745 MHz and 2.755 MHz are the least possible and greatest possible frequencies respectively.

46. least: 2350 cm^3 . greatest: 2450 cm^3 .

47. There are too many significant digits; time only has 2 significant digits.

48. $4.4s - 2.72s = 1.68s$

$= 1.7s$ to two significant digits
since $4.4s$ has the least number of significant digits (= 2).

49. (a) $2.2 + 3.8 \times 4.5 = 19.3$

(b) $(2.2 + 3.8) \times 4.5 = 27$

50. (a) $6.03 \div 2.25 + 1.77 = 2.68 + 1.77 = 4.45$

(b) $6.03 \div (2.25 - 1.77) = 6.03 \div 4.02 = 1.5$

51. (a) $2+0$
(b) $2-0$
(c) $0-2$

- (d) $2*0$
(e) $2/0$

- (e2) $\text{ERR:DIVIDE BY } 0$
1:quit
2:Goto

52. (a) $2 \div 0.0001 = 20,000$

$2 \div 0$, error

(b) $0.0001 \div 0.0001 = 1$

$0 \div 0$, error

(c) calculator will not divide by zero.

2/0.0001 20000
2/0
ERR:DIVIDE BY 0

ERR:DIVIDE BY 0
1:quit
2:Goto

0.0001/0.0001 1
0/0
ERR:DIVIDE BY 0

ERR:DIVIDE BY 0
1:quit
2:Goto

53. $61812311 \rightarrow X$
 61812311
 $11381216 \rightarrow Y$
 11381216
 $(X-Y)/9$
 5603455

54. $9*8+7+6+5+4+3+2+$
 $1+0$
100

- 55.** $\frac{22}{7} = 3.142857\dots$ which differs from π starting in the thousandths place ($\pi = 3.14159265\dots$).

(a) $3.1416 > \pi$ (b) $\frac{22}{7} > \pi$

56. (a) $\frac{8}{33} = 0.242424\dots = 0.\overline{24}$

(b) $\pi = 3.141592653589873\dots$

57. (a) $\frac{1}{3} = 0.333\dots$

(b) $\frac{5}{11} = 0.454545\dots$

(c) $\frac{2}{5} = 0.4000\dots$

0 is the repeating part

58. $\frac{124}{990} = 0.1252525\dots = 0.1\overline{25}$

$= 0.1252525253$, calculator last digit different because of calculator round-off

59. $32.4 + 26.704 + 36.23 = 95.3 \text{ MJ}$

60. $1450 - 938 = 512 \rightarrow 510 \text{ km/hr}$

61. $1 \text{ MB} = 1,048,576 \text{ bytes}$

$$\begin{aligned} 256 \text{ MB} &= 256 \times 1,048,576 \\ &= 268,435,456 \text{ bytes} \end{aligned}$$

62. $V = 3.55(15.2 + 5.64 + 101.23) = 433 \text{ V}$

63. $\frac{100(40.63 + 52.96)}{105.30 + 52.96} = 59.14\%$

64. $\frac{50.45(9.80)}{1 + \frac{100.9}{23}} = 92 \text{ N}$

1.4 Exponents

1. $(-x^3)^2 = [(-1)x^3]^2 = (-1)^2(x^3)^2 = x^{3(2)} = x^6$

2. $2x^0 = 2(1) = 2$

3. $\left(\frac{x}{a^3}\right)^{-2} = \frac{x^{-2}}{(a^3)^{-2}} = \frac{x^{-2}}{a^{-6}} = \frac{a^6}{x^2}$

4. $8 - (-1)^3 - 2(-3)^2 = 8 - (-1) - 2(9)$
 $= 9 - 18$
 $= -9$

5. $x^3 \cdot x^4 = x^{3+4} = x^7$

6. $y^2 y^7 = y^{2+7} = y^9$

7. $2b^4 b^2 = 2b^{4+2} = 2b^6$

8. $3k^5(k) = 3k^{5+1} = 3k^6$

9. $\frac{m^5}{m^3} = m^{5-3} = m^2$

10. $\frac{2x^6}{-x} = -2x^{6-1} = -2x^5$

11. $\frac{-n^5}{7n^9} = \frac{-n^{5-9}}{7} = \frac{-n^{-4}}{7} = \frac{-1}{7n^4}$

12. $\frac{3s}{s^4} = 3s^{1-4} = 3s^{-3} = \frac{3}{s^3}$

13. $(P^2)^4 = P^{2 \cdot 4} = P^8$ **14.** $(x^8)^3 = x^{8 \cdot 3} = x^{24}$

15. $(-2\pi)^3 = -2^3 \cdot \pi^3 = -8\pi^3$ **16.** $(-ax)^5 = -a^5 x^5$

17. $(aT^2)^{30} = a^{30} T^{2(30)} = a^{30} T^{60}$

18. $(3r^2)^3 = 3^3 r^{2 \cdot 3} = 27r^6$

19. $\left(\frac{2}{b}\right)^3 = \frac{2^3}{b^3} = \frac{8}{b^3}$

20. $\left(\frac{F}{t}\right)^{20} = \frac{F^{20}}{t^{20}}$

21. $\left(\frac{x^2}{-2}\right)^4 = \frac{x^{2 \cdot 4}}{2^4} = \frac{x^8}{16}$

22. $\left(\frac{3}{n^3}\right)^3 = \frac{3^3}{(n^3)^3} = \frac{27}{n^{3 \cdot 3}} = \frac{27}{n^9}$

23. $(8a)^0 = 1$

25. $-3x^0 = (-3)(1) = -3$

27. $6^{-1} = \frac{1}{6^1} = \frac{1}{6}$

29. $\frac{1}{R^{-2}} = R^2$

31. $(-t^2)^7 = -t^{2 \cdot 7} = -t^{14}$

32. $(-y^3)^5 = -y^{3 \cdot 5} = -y^{15}$

33. $(2v^2)^{-6} = (2^{-6})(v^{-2 \cdot 6}) = \frac{1}{64v^{12}}$

34. $-(-c^4)^{-4} = -\left((-1)^{-4}(c^4)^{-4}\right) = -c^{-4(4)}$
 $= -c^{-16}$
 $= -\frac{1}{c^{16}}$

35. $\frac{L^{-3}}{L^{-5}} = \frac{L^5}{L^3} = -L^2$

36. $2i^{40}i^{-70} = 2i^{-30} = \frac{2}{i^{30}}$

37. $\frac{2v^4}{(2v)^4} = \frac{2v^4}{2^4 v^4} = \frac{1}{2^3} = \frac{1}{8}$

38. $\frac{x^2 x^3}{(x^2)^3} = \frac{x^5}{x^6} = \frac{1}{x}$

39. $\frac{(n^2)^4}{(n^4)^2} = \frac{n^{2 \cdot 4}}{n^{4 \cdot 2}} = 1$ (since $2 \cdot 4 = 4 \cdot 2$)

40. $\frac{(3t)^{-1}}{3t^{-1}} = \frac{\frac{1}{3t}}{3 \cdot \frac{1}{t}} = \frac{1}{9}$

41. $\left(\pi^0 x^2 a^{-1}\right)^{-1} = \left(1 \cdot x^2 \cdot a^{-1}\right)^{-1} = x^{-2(1)} \left(a^{-1(-1)}\right)$
 $= \frac{a}{x^2}$

24. $-v^0 = -1$

26. $-(-2)^0 = -1$

28. $-w^{-5} = -\frac{1}{w^5}$

30. $\frac{1}{t^{-48}} = t^{48}$

42. $(3m^{-2}n^4)^{-2} = 3^{-2}m^4n^{-8} = \frac{m^4}{9n^8}$

43. $(-8g^{-1}s^3)^2 = (-8)^2 \cdot g^{-2} \cdot (s^3)^2 = \frac{64s^{3 \cdot 2}}{g^2} = \frac{64s^6}{g^2}$

44. $ax^{-2}(-a^2x)^2 = ax^{-2}a^4x^2 = a^5$

45. $\left(\frac{4x^{-1}}{a^{-1}}\right)^{-3} = \frac{4^{-3}x^{-1(-3)}}{a^{-1(-3)}} = \frac{x^3}{4^3 a^3} = \frac{x^3}{64a^3}$

46. $\left(\frac{2b^2}{-y^5}\right)^{-2} = \frac{2^{-2}b^{-4}}{(-y)^{-10}} = \frac{\frac{1}{4} \cdot \frac{1}{b^4}}{\frac{1}{y^{10}}} = \frac{y^{10}}{4b^4}$

47. $\frac{15n^2T^5}{3n^{-1}T^6} = \frac{5n^{2(-1)}}{T} = \frac{5n^3}{T}$

48. $\frac{(nRT^{-2})^{32}}{R^{-2}T^{32}} = \frac{n^{32}R^{32}T^{-64}}{R^{-2}T^{32}} = \frac{n^{32}R^{34}}{T^{96}}$

49. $7(-4) - (-5)^2 = -28 - 25 = -53$

50. $6 + |-2|^5 - (-2)(8) = 6 + 32 + 16 = 54$

51. $-(-26.5)^2 - (-9.85)^3 = 253$ (second term is precise to ones).

52. $-0.711^2 - (-|-0.809|)^6 = -0.711^2 - (-0.809)^6$
 $= -0.711^2 - (0.809)^6$
 $= -0.786$

53. $\frac{3.07(-|-1.86|)}{(-1.86)^4 + 1.596} = \frac{3.07(-1.86)}{1.86^4 + 1.596} = -0.421$

54. $\frac{15.66^2 - (-4.017)^4}{1.044(-3.68)} = 3.94$

55. $2.38(-60.7)^2 - \frac{2540}{1.17^3} + 0.806^5 (26.1^3 - 9.88^4)$
 $= 9990$
 (all three terms are precise to tens).

56. $0.513(-2.778) - (-3.67)^3 + \frac{0.889^4}{1.89 - 1.09^2} = 48.90$

57. $\left(\frac{1}{x^{-1}}\right)^{-1} = \frac{1^{-1}}{x^{-1(-1)}} = \frac{1}{x}$ reciprocal of x , yes.

58. $\left(\frac{0.2 - 5^{-1}}{10^{-2}}\right)^0 = \left(\frac{0}{0.01}\right)^0 = (0)^0 \neq 1$
 since $a^0 = 1$ requires $a \neq 0$.

59. $a^3 = 5$
 $(a^3)^4 = 5^4$
 $a^{3(4)} = 625$
 $a^{12} = 625$

60. If $a^{-2} < a^{-1}$ is true, then

$$\begin{aligned} \frac{1}{a^2} &< \frac{1}{a} \\ 1 &< \frac{a^2}{a} = a \\ a &> 1 > 0 \\ a &> 0, \text{ therefore} \end{aligned}$$

$a^{-2} < a^{-1}$ is not true for any negative value of a .

61. $(x^a \cdot x^{-a})^5 = (x^{a+(-a)})^5 = (x^0)^5$
 $= (1)^5, \quad x \neq 0$
 $= 1$

62. $(-y^{a-b} \cdot y^{a+b})^2 = (y^{a-b+a+b})^2 = (y^{2a})^2$
 $= y^{2a \cdot 2}$
 $= y^{4a}$

63. $\left(\frac{kT}{hc}\right)^3 (GkThc)^2 c = \frac{k^3 T^3}{h^3 c^3} G^2 k^2 T^2 h^2 c^2 c$
 $= \frac{G^2 k^5 T^5}{h}$

64. $(GmM)(mr)^{-1}(r^{-2}) = (GmM) \cdot \frac{1}{mr} \cdot \frac{1}{r^2}$
 $= \frac{GM}{r^3}$

65. $\pi \left(\frac{r}{2}\right)^3 \left(\frac{4}{3\pi r^2}\right) = \pi \cdot \frac{r^3}{8} \cdot \frac{4}{3\pi r^2} = \frac{r}{6}$

66. $\frac{gM (2\pi fM)^{-2}}{2\pi fC} = \frac{gM}{2\pi fC 4\pi^2 f^2 M^2}$
 $= \frac{g}{8\pi^3 f^3 CM}$

67. $2500(1 + 0.042/4)^{24} = \3212.27

68. $\frac{x(1000 - 20x^2 + x^3)}{1850}$
 $= \frac{6.85(1000 - 20 \times 6.85^2 + 6.85^3)}{1850}$
 $= 1.42 \text{ cm}$

69.

n	$\left(1 + \frac{1}{n}\right)^n$
1	2
10	2.59374246
100	2.704813829
1000	2.716923932

70. $1 \text{ TB} = 2^{10} \text{ GB} \left(\frac{2^{10} \text{ MB}}{\text{GB}} \right) \left(\frac{2^{10} \text{ bytes}}{\text{MB}} \right)$

$1 \text{ TB} = 2^{30} \text{ bytes}$

71. $2.5 \text{ ft} = 2.5 \text{ ft} \left(\frac{12 \text{ in.}}{\text{ft}} \right) = 30 \text{ in.}$

72. $0.225 \text{ km} = 0.225 \text{ ft} \left(\frac{1000 \text{ m}}{\text{km}} \right) \left(\frac{100 \text{ cm}}{\text{m}} \right)$
 $\left(\frac{\text{in.}}{2.54 \text{ cm}} \right) \left(\frac{\text{ft}}{12 \text{ in.}} \right)$
 $= 738 \text{ ft}$

$$73. \quad 65.2 \frac{\text{m}}{\text{s}} = 65.2 \frac{\text{m}}{\text{s}} \left(\frac{3600 \text{ s}}{\text{h}} \right) \left(\frac{100 \text{ cm}}{\text{m}} \right)$$

$$\left(\frac{\text{in.}}{2.54 \text{ cm}} \right) \left(\frac{\text{ft}}{12 \text{ in.}} \right) = 770,000 \frac{\text{ft}}{\text{h}}$$

$$74. \quad 7.25 \frac{\text{g}}{\text{cm}^2} = 7.25 \frac{\text{g}}{\text{cm}^2} \left(\frac{\text{kg}}{1000 \text{ g}} \right) \left(\frac{100^2 \text{ cm}^2}{\text{m}^2} \right)$$

$$= 72.5 \frac{\text{kg}}{\text{m}^2}$$

$$75. \quad 25.0 \frac{\text{mi}}{\text{gal}} = 25 \frac{\text{mi}}{\text{gal}} \left(\frac{\text{km}}{0.6214 \text{ mi}} \right) \left(\frac{\text{gal}}{4 \text{ qt}} \right) \left(\frac{1.057 \text{ qt}}{\text{L}} \right)$$

$$= 10.6 \frac{\text{km}}{\text{L}}$$

$$76. \quad 32.0 \frac{\text{ft}}{\text{s}^2} =$$

$$32.0 \frac{\text{ft}}{\text{s}^2} \left(\frac{60^2 \text{ s}^2}{\text{min}^2} \right) \left(\frac{12 \text{ in.}}{\text{ft}} \right) \left(\frac{2.54 \text{ cm}}{\text{in.}} \right) \left(\frac{\text{m}}{100 \text{ cm}} \right)$$

$$= 35,100 \frac{\text{m}}{\text{min}^2}$$

1.5 Scientific Notation

1. $8.06 \times 10^3 = 8060$

2. $750,000,000,000^{-1} = (7.50 \times 10^{11})^{-1}$

$$= 7.50^{-1} \times 10^{-11}$$

$$= 1.33 \times 10^{-12}$$

3. $4.5 \times 10^4 = 45,000$ 4. $6.8 \times 10^7 = 68,000,000$

5. $2.01 \times 10^{-3} = 0.00201$; move decimal point
3 places to the left by adding 2 zeros.

6. $9.61 \times 10^{-5} = 0.0000961$

7. $3.23 \times 10^0 = 3.23$ 8. $8 \times 10^0 = 8 \times 1 = 8$

9. $1.86 \times 10 = 18.6$; move decimal point 1 place
to the right.

10. $1 \times 10^{-1} = 0.1$ 11. $4000 = 4 \times 10^3$

12. $56,000 = 5.6 \times 10^4$

13. $0.0087 = 8.7 \times 10^{-3}$; move decimal point to
the right 3 places.

14. $0.7 = 7 \times 10^{-1}$ 15. $6.09 = 6.09 \times 10^0$

16. $10 = 1 \times 10^1$

17. $1 = 1.0 \times 10^0$

18. $0.0000908 = 9.08 \times 10^{-5}$

19. $28,000(2,000,000,000) = 2.8 \times 10^4 (2 \times 10^9)$
 $= 5.6 \times 10^{13}$

20. $50,000(0.006) = 300 = 3 \times 10^2$

21. $\frac{88,000}{0.0004} = \frac{8.8 \times 10^4}{4.0 \times 10^{-4}} = 2.2 \times 10^8$

22. $\frac{0.00003}{6,000,000} = 5 \times 10^{-12}$

23. $2 \times 10^{-35} + 3 \times 10^{-34} = 0.2 \times 10^{-34} + 3 \times 10^{-34}$
 $= 3.2 \times 10^{-34}$

24. $5.3 \times 10^{12} - 3.7 \times 10^{10} = 530 \times 10^{10} - 3.7 \times 10^{10}$
 $= 526.3 \times 10^{10}$
 $= 5.263 \times 10^{12}$

25. $(1.2 \times 10^{29})^3 = 1.2^3 \times 10^{29(3)}$
 $= 1.728 \times 10^{87}$

26. $(2 \times 10^{-16})^{-5} = 2^{-5} \times 10^{-16(-5)}$
 $= 0.03125 \times 10^{80}$
 $= 3.125 \times 10^{78}$

27. $1280(865,000)(43.8) = 4.85 \times 10^{10}$

28. $0.0000569(3,190,000) = 1.82 \times 10^2$

29. $\frac{0.0732(6710)}{0.00134(0.0231)} = \frac{7.32 \times 10^{-2} \times 6.71 \times 10^3}{1.34 \times 10^{-3} \times 2.31 \times 10^{-2}}$
 $= 1.59 \times 10^7$

30. $\frac{0.00452}{2430(97,100)} = 1.92 \times 10^{-11}$

31. $(3.642 \times 10^{-8})(2.736 \times 10^5) = 9.965 \times 10^{-3}$

32. $\frac{(7.309 \times 10^{-1})^2}{5.9843(2.5036 \times 10^{-20})} = 3.566 \times 10^{18}$

33. $\frac{(3.69 \times 10^{-7})(4.61 \times 10^{21})}{0.0504} = 3.38 \times 10^{16}$

34. $\frac{(9.9 \times 10^7)(1.08 \times 10^{12})^2}{(3.603 \times 10^{-5})(2054)} = 1.56 \times 10^{33}$

35. $6,500,000 \text{ kW} = 6.5 \times 10^6 \text{ kW}$

36. $60,000,000,000,000 \text{ bytes} = 6.0 \times 10^{13} \text{ bytes}$

37. $0.000003 \text{ W} = 3 \times 10^{-6} \text{ W}$

38. $0.0075 \text{ mm} = 7.5 \times 10^{-3} \text{ mm}$

39. $2,000,000,000 \text{ Hz} = 2 \times 10^9 \text{ Hz}$

40. $5 \times 10^{11} \text{ m}^3 = 500,000,000,000 \text{ m}^3$

41. $12,000,000,000 \text{ m}^2 = 1.2 \times 10^{10} \text{ m}^2$

42. $3.086 \times 10^{16} = 30,860,000,000,000,000 \text{ m}$

43. $1.6 \times 10^{-12} \text{ W} = 0.0000000000016 \text{ W}$

44. $2.4 \times 10^{43} = 0.000 \dots 00024 \text{ (42 zeros)}$

45. (a) $2300 = 2.3 \times 10^3$

(b) $0.23 = 230 \times 10^{-3}$

(c) $23 = 23 \times 10^0$

(d) $0.00023 = 230 \times 10^{-6}$

46. (a) $8,090,000 = 8.09 \times 10^6$

(b) $809,000 = 809 \times 10^3$

(c) $0.0809 = 80.9 \times 10^{-3}$

47. (a) $\text{google} = 1 \times 10^{100} = 10^{100}$

(b) $\text{googleplex} = 10^{\text{google}} = 10^{10^{100}}$

48. $\text{google} = N \cdot 10^{79}$

$10^{100} = N \cdot 10^{79}$

$$N = \frac{10^{100}}{10^{79}} = 10^{21}$$

A google is 10^{21} times greater than the number of electrons in the universe.

49. $1.4 \times 10^7 = 110 D_E$

$D_E = 1.3 \times 10^5 \text{ m}$

50.

$$\boxed{2^{30} \\ 1.073741824 \times 10^9}$$

51. $\frac{7.5 \times 10^{-15} \text{ s}}{\text{addition}} \cdot 5.6 \times 10^6 \text{ additions} = 4.2 \times 10^{-8} \text{ s}$

52. $0.085(0.00000000039) = 3.3 \times 10^{-11} \text{ mg}$

53. $\frac{4.57 \times 10^4}{1.86 \times 10^5} = 2.46 \times 10^{-1} \text{ s}$

54. (a) $1 \text{ day} = 1 \text{ day} \left(\frac{24 \text{ h}}{\text{day}} \right) \left(\frac{60 \text{ min}}{\text{h}} \right) \left(\frac{60 \text{ s}}{\text{min}} \right)$
 $= 8.64 \times 10^4 \text{ s}$

(b) $8.64 \times 10^4 \frac{\text{s}}{\text{day}}$
 $= 8.64 \times 10^4 \frac{\text{s}}{\text{day}} \cdot \frac{365.24 \text{ day}}{\text{year}} \cdot \frac{100 \text{ year}}{\text{century}}$
 $= 3.12 \frac{\text{s}}{\text{century}}$

55. mass

$$= 125,000,000 \text{ atoms} \left(\frac{16 \text{ amu}}{\text{atom}} \right) \left(\frac{1.66 \times 10^{-27}}{\text{amu}} \right)$$

 $= 3.32 \times 10^{-18} \text{ kg}$

56. $kT^4 = 0.000000057 \cdot 303^4 = 4.8 \times 10^2 \text{ W}$

57. $R = k / d^2$;
 $R = 0.00000002196 \div 0.00007998^2$
 $= 2196 \times 10^8 \div (7.998 \times 10^{-5})^2$
 $= 3.433 \Omega$

58. speed = $\frac{\text{distance}}{\text{time}} = \frac{149,600,000 \text{ km}}{499.0 \text{ s}}$
 $= 2.998 \times 10^5 \text{ km/s}$
 $2.998 \times 10^5 \frac{\text{km}}{\text{s}} \cdot 0.6214 \frac{\text{m}}{\text{km}} = 1.86 \times 10^5 \frac{\text{m}}{\text{s}}$,
same as Exercise 53.

1.6 Roots and Radicals

1. $-\sqrt[3]{64} = -4$ since $(-4)^3 = -64$

2. Changing $\sqrt{(25)(3)}$ to $\sqrt{(15)(5)}$ in $\sqrt{75}$
 $= \sqrt{(25)(3)}$ is not better since neither 15 nor
5 is a perfect square.

3. $\sqrt{16 \times 9} = \sqrt{16} \times \sqrt{9} = 4 \times 3 = 12$

4. $-\sqrt{-64}$ is imaginary, because the index is even.
No change required.

5. $\sqrt{81} = 9$

6. $\sqrt{225} = 15$

7. $-\sqrt{121} = -\sqrt{11^2} = -11$

8. $-\sqrt{36} = -6$

9. $-\sqrt{49} = -7$

10. $\sqrt{0.25} = \sqrt{\frac{1}{4}} = \frac{1}{2} = 0.5$

11. $\sqrt{0.09} = \sqrt{\frac{9}{100}} = \frac{3}{10} = 0.3$

12. $-\sqrt{900} = -30$

13. $\sqrt[3]{125} = 5$

14. $\sqrt[4]{16} = 2$

15. $\sqrt[3]{-126} = -6$

16. $-\sqrt[5]{-32} = -(-2) = 2$

17. $(\sqrt{5})^2 = 5$

18. $(\sqrt[3]{31})^3 = \sqrt[3]{31} \sqrt[3]{31} \sqrt[3]{31} = 31$

19. $(-\sqrt[3]{-47})^3 = (-1)^3 (\sqrt[3]{-47})^3 = -1(-47) = 47$

20. $(\sqrt[5]{-23})^5 = -23$

21. $(-\sqrt[4]{53})^4 = 53$

22. $-\sqrt{32} = -\sqrt{16 \cdot 2} = -4\sqrt{2}$

23. $\sqrt{1200} = \sqrt{400(3)} = 20\sqrt{3}$

24. $\sqrt{50} = \sqrt{25 \cdot 2} = 5\sqrt{2}$

25. $2\sqrt{84} = 2\sqrt{4 \cdot 21} = 2 \cdot 2\sqrt{21} = 4\sqrt{21}$

26. $\sqrt{\frac{108}{2}} = \sqrt{\frac{36 \cdot 3}{2}} = \frac{6\sqrt{3}}{2} = 3\sqrt{3}$

27. $\sqrt{\frac{80}{|3-7|}} = \sqrt{\frac{80}{4}} = \sqrt{20} = \sqrt{(4)(5)} = 2\sqrt{5}$

28. $\sqrt{81 \times 10^2} = \sqrt{81} \sqrt{10^2} = 9(10) = 90$

29. $\sqrt[3]{-8^2} = \sqrt[3]{-64} = -4$

30. $\sqrt[4]{9^2} = \sqrt[4]{81} = \sqrt[4]{3^4} = 3$

31. $\frac{7^2 \sqrt{81}}{(-3)^2 \sqrt{49}} = \frac{7^2 \times 9}{9 \times 7} = 7$

32. $\frac{2^5 \cdot \sqrt[5]{243}}{-3\sqrt{144}} = \frac{32 \cdot 3}{-3 \cdot 12} = \frac{-8}{3}$

33. $\sqrt{36 + 64} = \sqrt{100} = 10$

34. $\sqrt{25 + 144} = \sqrt{169} = 13$

35. $\sqrt{3^2 + 9^2} = \sqrt{9 + 81} = \sqrt{90} = \sqrt{9 \times 10} = 3\sqrt{10}$

36. $\sqrt{8^2 - 4^2} = \sqrt{64 - 16} = \sqrt{48} = \sqrt{16 \cdot 3} = 4\sqrt{3}$

37. $\sqrt{85.4} = 9.24$

38. $\sqrt{3762} = 61.34$

39. $\sqrt{0.4729} = 0.6877$

40. $\sqrt{0.0627} = 0.250$

41. (a) $\sqrt{1296 + 2304} = \sqrt{3600} = 60.00$

(b) $\sqrt{1296} = \sqrt{2304} = 36.00 + 48.00 = 84.00$

42. (a) $\sqrt{10.6276 + 2.1609} = \sqrt{12.7885} = 3.57610$
 (b) $\sqrt{10.6276} + \sqrt{2.1609} = 3.26 + 1.47 = 4.7300$

43. (a) $\sqrt{0.0429^2 - 0.183^2} = \sqrt{0.0150552}$
 $= 0.0388$
 (b) $\sqrt{0.0429^2} - \sqrt{0.0183^2} = 0.0429 - 0.0183$
 $= 0.0246$

44. (a) $\sqrt{3.625^2 + 0.614^2} = 3.677$
 (b) $\sqrt{3.625^2} + \sqrt{0.614^2} = 4.239$

45. $\sqrt{24s} = \sqrt{(24)(150)} = \sqrt{3600} = 60 \text{ mi/h}$

46. $\sqrt{Z^2 - X^2} = \sqrt{5.362^2 - 2.875^2} = 4.526\Omega$

47. $\sqrt{B/d} = \sqrt{2.18 \times 10^9 / 1.03 \times 10^3} = 1450 \text{ m/s}$

48. $\sqrt{40 \text{ m}} = \sqrt{(40)(75)} = \sqrt{3000} \approx 55 \text{ m/s}$

49. $d = \sqrt{w^2 + h^2} = \sqrt{52.3^2 + 29.3^2} = 59.9 \text{ in.}$

50. ARD = $100 \left(1 - \sqrt{\frac{V}{C}} \right) = 100 \left(1 - \sqrt{\frac{24,000}{38,000}} \right) = 21\%$

51. $v = \sqrt{gd} = \sqrt{9.8(3500)} \cdot \frac{\text{m}}{\text{s}} \cdot \frac{3600\text{s}}{\text{h}} \cdot \frac{\text{km}}{1000 \text{ m}}$
 $v = 670 \frac{\text{km}}{\text{h}}$

52. $d = \sqrt{1.27 \times 10^4 (9500) + 9500^2}$
 $d = 1.45 \times 10^4 \text{ km}$

53. No, it is not true if $a < 0$. It is always true that $\sqrt{a^2} = |a|$.

54. (a) \sqrt{x} requires $x \geq 0$
 $x > \sqrt{x} \geq 0 \Rightarrow x^2 > x \Rightarrow x(x-1) > 0 \Rightarrow x > 1$
 $x > \sqrt{x}$ for $x > 1$
 (b) $x = \sqrt{x} \Rightarrow x^2 = x \Rightarrow x(x-1) = 0 \Rightarrow x = 0, x = 1$
 $x = \sqrt{x}$ for $x = 0, x = 1$
 (c) $0 \leq x < \sqrt{x} \Rightarrow x^2 < x \Rightarrow x(x-1) < 0 \Rightarrow x < 1$
 $x < \sqrt{x}$ for $0 < x < 1$

55. $\begin{array}{r} \sqrt[3]{2140} \\ 12.88658743 \\ \hline \end{array}$
 $\begin{array}{r} \sqrt[3]{-0.214} \\ -.598142403 \\ \hline \end{array}$

56. $\begin{array}{r} \sqrt[7]{0.382} \\ .8715549346 \\ \hline \end{array}$
 $\begin{array}{r} \sqrt[7]{-382} \\ -2.338116758 \\ \hline \end{array}$

57. (a) imaginary (b) real

$\begin{array}{r} \sqrt{-64} \\ 8i \\ \hline \end{array}$
 $\begin{array}{r} \sqrt[4]{-64} \\ -4 \\ \hline \end{array}$

58 (a) real (b) imaginary

$\begin{array}{r} \sqrt[5]{-32} \\ -2 \\ \hline \end{array}$
 $\begin{array}{r} \sqrt[4]{-64} \\ 2+2i \\ \hline \end{array}$

1.7 Addition and Subtraction of Algebraic Expressions

1. $3x + 2y - 5y = 3x - 3y$

2. $3c - (2b - c) = 3c - 2b + c = -2b + 4c$

$$\begin{aligned} 3. \quad 3ax - [(ax - 5s) - 2ax] &= 3ax - [ax - 5s - 2ax] \\ &= 3ax - [-ax - 5s] \\ &= 3ax + ax + 5s \\ &= 4ax + 5s \end{aligned}$$

$$\begin{aligned} 4. \quad 3a^2b - \{a - [2a^2b - (a + 2b)]\} &= 3a^2b - \{a - [2a^2b - a - 2b]\} \\ &= 3a^2b - \{a - 2a^2b + a + 2b\} \\ &= 3a^2b - \{2a - 2a^2b + 2b\} \\ &= 3a^2b - 2a + 2a^2b - 2b \\ &= 5a^2b - 2a - 2b \end{aligned}$$

5. $5x + 7x - 4x = 12x - 4x = 8x$

6. $6t - 3t - 4t = -t$

7. $2y - y + 4x = y(2 - 1) + 4x = y + 4x$

8. $4C + L - 6C = -2C + L$

9. $2F - 2T - 2 + 3F - T = 5F - 3T - 2$

10. $x - 2y - 3x - y + z = -2x - 3y + z$

11. $a^2b - a^2b^2 - 2a^2b = a^2b - 2a^2b - a^2b^2 = -a^2b - a^2b^2$

12. $-xy^2 - 3x^2y^2 + 2xy^2 = xy^2 - 3x^2y^2$

13. $s + 3a - 4 - 2 = s + (2a - 4) = 3s - 4$

14. $5 + (3 - 4n + p) = 5 + 3 - 4n + p = -4n + p + 8$

15. $v - (4 - 5x + 2v) = v - 4 + 5x - 2v = 5x - v - 4$

$$\begin{aligned} 16. \quad -2a - \frac{1}{2}(b - a) &= -2a - \frac{1}{2}b + \frac{1}{2}a \\ &= -\frac{3}{2}a - \frac{1}{2}b \end{aligned}$$

17. $2 - 3 - (4 - 5a) = -1 - 4 + 5a = -5 + 5a = 5a - 5$

$$\begin{aligned} 18. \quad \sqrt{A} + (h - 2\sqrt{A}) - 3\sqrt{A} &= \sqrt{A} + h - 2\sqrt{A} - 3\sqrt{A} \\ &= h - 4\sqrt{A} \end{aligned}$$

19. $(a - 3) + (5 - 6a) = a - 3 + 5 - 6a = -5a + 2$

20. $(4x - y) - (-2x - 4y) = 4x - y + 2x + 4y = 6x + 3y$

21. $-(t - 2u) + (3u - t) = -t + 2u + 3u - t = 5u - 2t$

22. $2(x - 2y) + (5x - y) = 2x - 4y + 5x - y = 7x - 5y$

23. $3(2r + s) - (-5s - r) = 6r + 3s + 5s + r = 7r + 8s$

24. $3(a - b) - 2(a - 2b) = 3a - 3b - 2a + 4b = a + b$

$$\begin{aligned} 25. \quad -7(6 - 3j) - 2(j + 4) &= -42 + 21j - 2j - 8 \\ &= 19j - 50 \end{aligned}$$

$$\begin{aligned} 26. \quad -(5t + a^2) - 2(3a^2 - 2st) &= -5t - a^2 - 6a^2 + 4st \\ &= -7a^2 + 4st - 5t \end{aligned}$$

$$\begin{aligned} 27. \quad -[(6 - n) - (2n - 3)] &= -[6 - n - 2n + 3] \\ &= -6 + n + 2n - 3 \\ &= -9 + 3n \end{aligned}$$

$$\begin{aligned} 28. \quad -[(A - B) - (B - A)] &= -[A - B - B + A] \\ &= -[2A - 2B] \\ &= -2A + 2B \end{aligned}$$

29. $2[4 - (t^2 - 5)] = 2[4 - t^2 + 5] = 2[9 - t^2] = 18 - 2t^2$

$$\begin{aligned} 30. \quad -3\left[-3 - \frac{2}{3}(-a - 4)\right] &= -3\left[-3 + \frac{2}{3}a + \frac{8}{3}\right] \\ &= -3\left[\frac{2}{3}a - \frac{1}{3}\right] \\ &= -2a + 1 \end{aligned}$$

$$\begin{aligned}
 31. \quad -2[-x-2a-(a-x)] &= -2[-x-2a-a+x] \\
 &= 2x+4a+2a-2x \\
 &= 6a
 \end{aligned}$$

$$\begin{aligned}
 32. \quad -2[-3(x-2y)+4y] &= -2[-3x+6y+4y] \\
 &= -2[-3x+10y] \\
 &= 6x-20y
 \end{aligned}$$

$$\begin{aligned}
 33. \quad aZ-[3-(aZ+4)] &= aZ-[3-aZ-4] \\
 aZ-[-1-aZ] &= aZ+1+aZ \\
 &= 2aZ+1
 \end{aligned}$$

$$\begin{aligned}
 34. \quad 9v-[6-(-v-4)+4v] &= 9v-[6+v+4+4v] \\
 &= 9v-[5v+10]=9v-5v-10 \\
 &= 4v-10
 \end{aligned}$$

$$\begin{aligned}
 35. \quad 8c-\{5-[2-(3+4c)]\} &= 8c-\{5-[2-3-4c]\} \\
 &= 8c-\{5-2+3+4c\} \\
 &= 8c-5+2-3-4c=4c-6
 \end{aligned}$$

$$\begin{aligned}
 36. \quad 7y-\{y-[2y-(x-y)]\} &= 7y-\{y-[2y-x+y]\} \\
 &= 7y-\{y-2y+x-y\} \\
 &= 7y+2y-x \\
 &= 9y-x
 \end{aligned}$$

$$\begin{aligned}
 37. \quad 5p-(q-2p)-[3q-(p-q)] &= 5p-q+2p-[3q-p+q] \\
 &= 7p-q-[4q-p] \\
 &= 7p-q-4q+p \\
 &= 8p-5q
 \end{aligned}$$

$$\begin{aligned}
 38. \quad -(4-LC)-[(5LC-7)-(6LC+2)] &= -4+LC-[5LC-7-6LC-2] \\
 &= -4+LC-[-LC-9] \\
 &= -4+LC+LC+9 \\
 &= 2LC+5
 \end{aligned}$$

$$\begin{aligned}
 39. \quad -2\{-(4-x^2)-[3+(4-x^2)]\} &= -2\{-4+x^2-3-4+x^2\} \\
 &= 8-2x^2+6+8-2x^2 \\
 &= -4x^2+22
 \end{aligned}$$

$$\begin{aligned}
 40. \quad -\{[-(x-2a)-b]- (a-x)\} &= -\{[-x+2a-b]-a+x\} \\
 &= -\{x-2a+b-a+x\} \\
 &= -\{2x-3a+b\} \\
 &= -2x+3a+b
 \end{aligned}$$

$$\begin{aligned}
 41. \quad 5V^2-(6-(2V^2+3)) &= 5V^2-(6-2V^3-3) \\
 &= 5V^2-(3-2V^2) \\
 &= 5V^2-3+2V^2 \\
 &= 7V^2-3
 \end{aligned}$$

$$\begin{aligned}
 42. \quad -2F+2((2F-1)-5) &= -2F+2(2F-1-5) \\
 &= -2F+2(2F-6) \\
 &= -2F+4F-12 \\
 &= 2F-12
 \end{aligned}$$

$$\begin{aligned}
 43. \quad -(3t-(7+2t-(5t-6))) &= -(3t-7-2t+5t-6) \\
 &= -3t+7+2t-5t+6 \\
 &= -6t+13
 \end{aligned}$$

$$\begin{aligned}
 44. \quad a^2-2(x-5-(7-2(a^2-2x)-3x)) &= a^2-2(x-5-(7-2a^2+4x-3x)) \\
 &= a^2-2(x-5-(7-2a^2+x)) \\
 &= a^2-2(x-5-7+2a^2-x) \\
 &= a^2-2(2a^2-12) \\
 &= a^2-4a^2+24 \\
 &= -3a^2+24
 \end{aligned}$$

$$\begin{aligned}
 45. \quad -4[4R-2.5(Z-2R)-1.5(2R-Z)] &= -4[4R-2.5Z+5R-3R+1.5Z] \\
 &= -4[6R-Z] \\
 &= -24R+4Z \\
 &= 4Z-24R
 \end{aligned}$$

$$\begin{aligned}
 46. \quad & -3\{2.1e - 1.3(-f - 2(e - 5f))\} \\
 &= -3\{2.1e - 1.3(-f - 2e + 10f)\} \\
 &= -3\{2.1e - 1.3(-2e + 9f)\} \\
 &= -3\{2.1e + 2.6e - 11.7f\} \\
 &= -3\{4.7e - 11.7f\} \\
 &= -14.1e + 35.1f
 \end{aligned}$$

$$47. \quad 3D - (D - d) = 3D - D + d = 2D + d$$

$$48. \quad i_1 - (2 - 3i_2) + i_2 = i_1 - 2 + 3i_2 + i_2 = i_1 + 4i_2 - 2$$

$$\begin{aligned}
 49. \quad & \left[\left(B + \frac{4}{3}\alpha \right) + 2 \left(B - \frac{2}{3}\alpha \right) \right] \\
 & - \left[\left(B + \frac{4}{3}\alpha \right) - \left(B - \frac{2}{3}\alpha \right) \right] \\
 &= \left[B + \frac{4}{3}\alpha + 2B - \frac{4}{3}\alpha \right] - \left[B + \frac{4}{3}\alpha - B + \frac{2}{3}\alpha \right] \\
 &= [3B] - \left[\frac{6}{3}\alpha \right] = 3B - 2\alpha
 \end{aligned}$$

$$\begin{aligned}
 50. \quad \text{distance} &= 30(t-1) + 40(t+2) \\
 &= 30t - 30 + 40t + 80 \\
 &= 70t + 50
 \end{aligned}$$

$$\begin{aligned}
 51. \quad 15x + 25(x+10) &= 15x + 25x + 250 \\
 &= 40x + 250
 \end{aligned}$$

$$\begin{aligned}
 52. \quad & 2(2n+1)(30) - 2(n-2)(20) \\
 &= 60(2n+1) - 40(n-2) \\
 &= 120n + 60 - 40n + 80 \\
 &= 80n + 140 \text{ dollars}
 \end{aligned}$$

$$\begin{aligned}
 53. \quad (a) \quad & 2x^2 - y + 2a + 3y - x^2 - b = x^2 + 2y + 2a - b \\
 (b) \quad & 2x^2 - y + 2a - (3y - x^2 - b) \\
 &= 2x^2 - y + 2a - 3y + x^2 + b \\
 &= 3x^2 - 4y + 2a + b
 \end{aligned}$$

$$\begin{aligned}
 54. \quad & 3a^2 + b - c^3 + 2c^3 - 2b - a^2 - (4c^3 - 4b + 3) \\
 &= 2a^2 - b + c^3 - 4c^3 + 4b - 3 \\
 &= 2a^2 + 3b - 3c^3 - 3
 \end{aligned}$$

55. No, it should be

$$\begin{aligned}
 2x - 3y + 5 - (4x - y + 3) &= 2x - 3y + 5 - 4x + y - 3 \\
 &= -2x - 2y + 2
 \end{aligned}$$

56. No, it should be

$$\begin{aligned}
 2a - 3b - 4c - (-5a + 3b - 2c) \\
 &= 2a - 3b - 4c + 5a - 3b + 2c \\
 &= 7a - 6b - 2c
 \end{aligned}$$

$$57. \quad 3 - 5x < 0 \Rightarrow |3 - 5x| = -(3 - 5x)$$

$$\begin{aligned}
 5x - |3 - 5x| &= 5x - (-(3 - 5x)) \\
 &= 5x + 3 - 5x \\
 &= 3
 \end{aligned}$$

$$58. \quad 4 - x < 0$$

$$3 - x < -1 < 0 \Rightarrow |3 - x| = -(3 - x)$$

$$\begin{aligned}
 2 - x < -2 < 0 \Rightarrow |2 - x| &= -(2 - x) \\
 |3 - x| - |2 - x| &= -(3 - x) - (-(2 - x)) \\
 &= -3 + x + 2 - x \\
 &= -1
 \end{aligned}$$

$$59. \quad |a - b| = |-(a + b)| = |-(b - a)|$$

$$\begin{aligned}
 &= |(-1)(b - a)| \text{ and since } |ab| = |a| \cdot |b| \\
 &= |-1| \cdot |b - a| = 1 \cdot |b - a| \\
 &= |b - a|
 \end{aligned}$$

Yes, it is true that $|a - b| = |b - a|$.

60. Subtraction is not associative as shown by the counterexample $(5 - 4) - 3 \neq 5 - (4 - 3)$

$$1 - 3 \neq 5 - 1$$

$$-2 \neq 4$$

1.8 Multiplication of Algebraic Expressions

$$\begin{aligned} \text{1. } 2s^3(-st^4)^3(4s^2t) &= 2s^3(-s)^3(t^4)^3(4s^2t) \\ &= -2s^6t^{12}(4s^2t) \\ &= -8s^8t^{13} \end{aligned}$$

$$\begin{aligned} \text{2. } -2ax(3ax^2 - 4yz) &= (-2ax)(3ax^2) - (-2ax)(4yz) \\ &= -6a^2x^3 + 8axyz \end{aligned}$$

$$\begin{aligned} \text{3. } (x-2)(x-3) &= x^2 - 3x - 2x + 6 \\ &= x^2 - 5x + 6 \end{aligned}$$

$$\begin{aligned} \text{4. } (2a-b)^2 &= (2a-b)(2a-b) \\ &= 4a^2 - 2ab - 2ab + b^2 \\ &= 4a^2 - 4ab + b^2 \end{aligned}$$

$$\text{5. } (a^2)(ax) = a^{2+1}x = a^3x$$

$$\text{6. } (2xy)(x^2y^3) = 2x^3y^4$$

$$\begin{aligned} \text{7. } -ac^2(acx^3) &= (-1)(a^1)(c^2)(a^1)(c^1)(x^3) \\ &= (-1)a^2c^3x^3 \\ &= -a^2c^3x^3 \end{aligned}$$

$$\text{8. } -2cs^2(-4cs)^2 = -2cs^2(16c^2s^2) = -32s^4c^3$$

$$\text{9. } (2ax^2)^2(-2ax) = 4a^2x^4(-2ax) = -8a^3x^5$$

$$\text{10. } 6pq^3(3pq^2)^2 = 6pq^3(9p^2q^4) = 54p^3q^7$$

$$\text{11. } i^2(R+2r) = i^2R + 2i^2r$$

$$\text{12. } 2x(-p-q) = -2px - 2qx$$

$$\text{13. } -3s(s^2 - 5t) = -3s(s^2) + 3s(5t) = -3s^2 + 15st$$

$$\text{14. } -3b(2b^2 - b) = -6b^3 + 3b^2$$

$$\text{15. } 5m(m^2n + 3mn) = 5m^3n + 15m^2n$$

$$\text{16. } a^2bc(2ac - 3b^2c) = 2a^3bc^2 - 3a^2b^3c^2$$

$$\begin{aligned} \text{17. } 3M(-M - N + 2) &= 3M(-M) + 3M(-N) + 3M(2) \\ &= -3M^2 - 3MN + 6M \end{aligned}$$

$$\text{18. } -4c^2(-9gc - 2c + g^2) = 36gc^3 + 8c^3 - 4g^2c^2$$

$$\begin{aligned} \text{19. } ax(cx^2)(x + y^3) &= ax(cx^2(x) + cx^2(y^3)) \\ &= ax(cx^3) + ax(cx^2y^3) \\ &= acx^4 + acx^3y^3 \end{aligned}$$

$$\text{20. } -2(-3st^3)(3s - 4t) = 6st^3(3s - 4t) = 18s^2t^3 - 24st^4$$

$$\text{21. } (x-3)(x+5) = x^2 + 5x - 3x - 15 = x^2 + 2x - 15$$

$$\text{22. } (a+7)(a+1) = a^2 + 8a + 7$$

$$\begin{aligned} \text{23. } (x+5)(2x-1) &= x(2x) + x(-1) + 5(2x) + 5(-1) \\ &= 2x^2 - x + 10x - 5 \\ &= 2x^2 + 9x - 5 \end{aligned}$$

$$\text{24. } (4t_1 + t_2)(2t_1 - 3t_2) = 8t_1^2 - 10t_1t_2 + 3t_2^2$$

$$\begin{aligned} \text{25. } (2a-b)(-2b+3a) &= 6a^2 - 4ab - 3ab + 2b^2 \\ &= 6a^2 - 7ab + 2b^2 \end{aligned}$$

$$\text{26. } (-3 + 4w^2)(3w^2 - 1) = 12w^4 - 13w^2 + 3$$

$$\begin{aligned} \text{27. } (2s + 7t)(3s - 5t) &= 2s(3s) + 2s(-5t) + 7t(3s) + 7t(-5t) \\ &= 6s^2 - 10st + 21st - 35t^2 \\ &= 6s^2 + 11st - 35t^2 \end{aligned}$$

$$\text{28. } (5p - 2q)(p + 8q) = 5p^2 + 38pq - 16q^2$$

$$\text{29. } (x^2 - 1)(2x + 5) = 2x^3 + 5x^2 - 2x - 5$$

$$\text{30. } (3y^2 + 2)(2y - 9) = 6y^3 - 27y^2 + 4y - 18$$

$$\begin{aligned} \text{31. } (x - 2y - 4)(x - 2y + 4) &= x^2 - 2xy + 4x - 2xy + 4y^2 - 8y - 4x + 8y - 16 \\ &= x^2 + 4y^2 - 4xy - 16 \end{aligned}$$

32. $(2a+3b+1)(2a+3b-1)$

$$\begin{aligned} &= 4a^2 + 6ab - 2a + 6ab + 9b^2 - 3b + 2a + 3b - 1 \\ &= 4a^2 + 9b^2 + 12ab - 1 \end{aligned}$$

33. $2(a+1)(a-9) = 2(a^2 - 8a - 9) = 2a^2 - 16a - 18$

34. $-5(y-3)(y+6) = -5(y^2 + 3y - 18)$
 $= -5y^2 - 15y + 90$

35. $-3(3-2T)(3T+2) = (-9+6T)(3T+2)$
 $= -27T - 18 + 18T^2 + 12T$
 $= 18T^2 - 15T - 18$

36. $2n(5-n)(6n+5) = (10n - 2n^2)(6n+5)$
 $= 60n^2 + 50n - 12n^3 - 10n^2$
 $= -12n^3 + 50n^2 + 50n$

37. $2L(L+1)(4-L) = 2L(4L - L^2 + 4 - L)$
 $= 2L(-L^2 + 3L + 4)$
 $= -2L^3 + 6L^2 + 8L$

38. $ax(x+4)(7-x^2) = ax(7x - x^3 + 28 - 4x^2)$
 $= 7ax^2 - ax^4 + 28ax - 4ax^3$

39. $(2x-5)^2 = 4x^2 - 20x + 25$

40. $(x-3y)^2 = x^2 - 6xy + 9y^2$

41. $(x_1 + 3x_2)^2 = (x_1 + 3x_2)(x_1 + 3x_2)$
 $= x_1^2 + 3x_1x_2 + 3x_1x_2 + 9x_2^2$
 $= x_1^2 + 6x_1x_2 + 9x_2^2$

42. $(7m+1)^2 = 49m^2 + 14m + 1$

43. $(xyz-2)^2 = x^2y^2z^2 - 4xyz + 4$

44. $(b-6x^2)^2 = b^2 - 2(b)(6x^2) + (6x^2)^2$
 $= b^2 - 12bx^2 + 36x^4$

45. $2(x+8)^2 = 2(x^2 + 16x + 64) = 2x^2 + 32x + 128$

46. $3(3R+4)^2 = 3(9R^2 + 24R + 16) = 27R^2 + 72R + 48$

47. $(2+x)(3-x)(x-1) = (6+x-x^2)(x-1)$
 $= 6x - 6 + x^2 - x - x^3 + x^2$
 $= -x^3 + 2x^2 + 5x - 6$

48. $(3x-c^2)^3 = (9x^2 - 6xc^2 + c^4) \cdot (3x - c^2)$
 $= 27x^3 - 9x^2c^2 - 18x^2c^2 + 6xc^4 + 3xc^4 - c^6$
 $= 27x^3 - 27x^2c^2 + 9xc^4 - c^6$

49. $3T(T+2)(2T-1) = (3T^2 + 6T)(2T-1)$
 $= 6T^3 - 3T^2 + 12T^2 - 6T$
 $= 6T^3 + 9T^2 - 6T$

50. $\left[(x-2)^2 (x+2) \right]^2 = \left[(x^2 - 4x + 4)(x+2) \right]^2$
 $= \left[x^3 + 2x^2 - 4x^2 - 8x + 4x + 8 \right]^2$
 $= (x^3 - 2x^2 - 4x + 8)(x^3 - 2x^2 - 4x + 8)$
 $= x^6 - 2x^5 - 4x^4 + 8x^3 - 2x^5 + 4x^4 + 8x^3 - 16$
 $- 4x^4 + 8x^3 + 16x^2 - 32x + 8x^3 - 16x^2 - 32x + 64$
 $= x^6 - 4x^5 - 4x^4 + 32x^3 - 16x^2 - 64x + 64$

51. (a) For $x = 3, y = 4$,

$$\begin{aligned} (x+y)^2 &= (3+4)^2 = 7^2 = 49 \\ x^2 + y^2 &= 3^2 + 4^2 = 9 + 16 = 25 \end{aligned}$$

which shows $(x+y)^2 \neq x^2 + y^2$.

(b) For $x = 3, y = 4$,

$$\begin{aligned} (x-y)^2 &= (3-4)^2 = (-1)^2 = 1 \\ x^2 - y^2 &= 3^2 - 4^2 = 9 - 16 = -7 \end{aligned}$$

which shows $(x-y)^2 \neq x^2 - y^2$.

52. $(98)(102) = (100-2)(100+2) = 100^2 - 2^2$
 $= 10,000 - 4 = 9996$

53. No, it should be

$$\begin{aligned} (x^2)(x^4) + (x^3)^5 &= x^{2+4} + x^{3(5)} \\ &= x^6 + x^{15} \end{aligned}$$

54. No, it should be

$$\begin{aligned} & \left[(x^3)(x^2) \right]^2 + \left[x(x^4) \right]^2 = [x^5]^2 + [x^5]^2 \\ &= x^{10} + x^{10} \\ &= 2x^{10} \end{aligned}$$

55. Let $1 < n < 9$, $n^2 - 1 = (n-1)(n+1)$ which shows the square of the integer minus 1 = product of the integer before n and the integer after n .

$$\begin{aligned} 56. & (x-2)(x+3)(x+2)(x-3) \\ &= (x-2)(x+2)(x+3)(x-3) \\ &= (x^2 - 4)(x^2 - 9) \\ &= x^4 - 9x^2 - 4x^2 + 36 \\ &= x^4 - 13x^2 + 36 \end{aligned}$$

$$\begin{aligned} 57. & (x+y)^3 = (x+y)(x+y)(x+y) \\ &= (x^2 + 2xy + y^2)(x+y) \\ &= x^3 + x^2y + 2x^2y + 2xy^2 + xy^2 + y^3 \\ &= x^3 + 3x^2y + 3xy^2 + y^3 \neq x^3 + y^3 \end{aligned}$$

$$\begin{aligned} 58. & (x+y)(x^2 - xy + y^2) \\ &= x^3 - x^2y + xy^2 + x^2y - xy^2 + y^3 \\ &= x^3 + y^3 \end{aligned}$$

$$\begin{aligned} 59. & P(1+0.01r)^2 = P(1+0.02r+0.0001r^2) \\ &= P + 0.02Pr + 0.0001Pr^2 \end{aligned}$$

$$\begin{aligned} 60. & 1000(1+0.0025r)^2 \\ &= 1000(1+0.005r+0.00000625r^2) \\ &= 1000 + 5r + 0.00625r^2 \end{aligned}$$

$$\begin{aligned} 61. & (2R-X)^2 - (R^2 + X^2) \\ &= 4R^2 - 4RX + X^2 - R^2 - X^2 \\ &= 3R^2 - 4RX \end{aligned}$$

$$\begin{aligned} 62. & (2T^3 + 3)(T^2 - T - 3) \\ &= 2T^5 - 2T^4 - 6T^3 + 3T^2 - 3T - 9 \end{aligned}$$

$$\begin{aligned} 63. & (n+100)^2 = n^2 + 200n + 100^2 \\ &= n^2 + 200n + 10,000 \end{aligned}$$

$$\begin{aligned} 64. & (T^2 - 100)(T - 10)(T + 10) \\ &= (T^2 - 100)(T^2 - 100) \\ &= T^4 - 100T^2 - 100T^2 + 100^2 \\ &= T^4 - 200T^2 + 10,000 \end{aligned}$$

$$\begin{aligned} 65. & (R_1 + R_2)^2 - 2R_2(R_1 + R_2) \\ &= R_1^2 + 2R_1R_2 + R_2^2 - 2R_1R_2 - 2R_2^2 \\ &= R_1^2 - R_2^2 \end{aligned}$$

$$\begin{aligned} 66. & 27x^2 - 24(x-6)^2 - (x-12)^3 \\ &= 27x^2 - 24(x^2 - 12x + 36) \\ &\quad - (x^3 - 36x^2 + 432x - 1728) \\ &= 27x^2 - 24x^2 + 288x - 864 - x^3 + 36x^2 \\ &\quad - 432x + 1728 \\ &= -x^3 + 39x^2 - 144x + 864 \end{aligned}$$

1.9 Division of Algebraic Expressions

$$1. \frac{-6a^2xy^2}{-2a^2xy^5} = 3y^{2-5} = 3y^{-3} = \frac{3}{y^3}$$

$$\begin{aligned} 2. & \frac{4x^3y - 8x^3y^2 + 2x^2y}{2xy^2} = \frac{4x^3y}{2xy^2} - \frac{8x^3y^2}{2xy^2} + \frac{2x^2y}{2xy^2} \\ &= \frac{2x^2}{y} - 4x^2 + \frac{x}{y} \end{aligned}$$

$$\begin{array}{r} 3x-2 \\ \hline 2x-1 \overline{)6x^2-7x+2} \\ 6x^2-3x \\ \hline -4x+2 \\ \hline -4x+2 \\ \hline 0 \end{array}$$

$$4x^2 - 1 \overline{)8x^3 - 4x^2 + 0x + 3}$$

$$\begin{array}{r} 2x - 1 \\ 8x^3 \\ - 2x \\ \hline - 4x^2 + 2x + 3 \\ - 4x^2 \quad \quad + 1 \\ \hline 2x + 2 \end{array}$$

$$\frac{8x^3 - 4x^2 + 3}{4x^2 - 1} = 2x - 1 + \frac{2x + 2}{4x^2 - 1}$$

$$5. \frac{8x^3 y^2}{-2xy} = -4x^2 y$$

$$6. \frac{-18b^7 c^3}{bc^2} = -18b^6 c$$

$$7. \frac{-16r^3 t^5}{-4r^5 t} = \frac{4t^{5-1}}{r^{5-3}} = \frac{4t^4}{r^2}$$

$$8. \frac{51mn^5}{17m^2 n^2} = \frac{3n^3}{m}$$

$$9. \frac{(15x^2)(4bx)(2y)}{30bxy} = 4x^2$$

$$10. \frac{(5sT)(8s^2 T^3)}{10s^3 T^2} = \frac{40s^3 T^4}{10s^3 T^2} = 4T^2$$

$$11. \frac{6(ax)^2}{-ax^2} = \frac{6a^2 x^2}{-ax^2} = -6a^{2-1} x^{2-2} = -6a$$

$$12. \frac{12a^2 b}{(3ab^2)} = \frac{12a^2 b}{9a^2 b^4} = \frac{4}{3b^3}$$

$$13. \frac{3a^2 x + 6xy}{3x} = \frac{3a^2 x}{3x} + \frac{6xy}{3x} = a^2 + 2y$$

$$14. \frac{2m^2 n - 6mn}{-2m} = \frac{2m^2 n}{-2m} - \frac{6mn}{-2m} = -mn + 3n$$

$$15. \frac{3rst - 6r^2 st^2}{3rs} = \frac{3rst}{3rs} - \frac{6r^2 st^2}{3rs} = t - 2rt^2$$

$$16. \frac{-5a^2 n - 10an^2}{5an} = \frac{-5a^2 n}{5ab} - \frac{10an^2}{5an} = -a - 2n$$

$$17. \frac{4pq^3 + 8p^2 q^2 - 16pq^5}{4pq^2} = \frac{4pq^3}{4pq^2} + \frac{8p^2 q^2}{4pq^2} - \frac{16pq^5}{4pq^2} \\ = q + 2p - 4q^3$$

$$18. \frac{a^2 x_1 x_2^2 + ax_1^3 - ax_1}{ax_1} = \frac{a^2 x_1 x_2^2}{ax_1} + \frac{ax_1^3}{ax_1} - \frac{ax_1}{ax_1} \\ = ax_2^2 + x_1^2 - 1$$

$$19. \frac{2\pi fL - \pi fR^2}{\pi fR} = \frac{2\pi fL}{\pi fR} - \frac{\pi fR^2}{\pi fR} = \frac{2L}{R} - R$$

$$20. \frac{9(aB)^4 - 6aB^4}{-3aB^3} = \frac{9a^4 B^4}{-3aB^3} - \frac{6aB^4}{-3aB^3} = -3a^3 B + 2B$$

$$21. \frac{-3ab^2 + 6ab^3 - 9a^2 b^2}{-9a^2 b^2} = \frac{3ab^2}{9a^2 b^2} - \frac{6ab^3}{9a^2 b^2} + \frac{9a^2 b^2}{9a^2 b^2} \\ = \frac{1}{3a} - \frac{2b}{3a} + 1$$

$$22. \frac{2x^{n+2} + 4ax^n}{2x^n} = \frac{2x^n x^2}{2x^n} + \frac{4ax^n}{2x^n} = x^2 + 2a$$

$$23. \frac{6y^{2n} - 4ay^{n+1}}{2y^n} = \frac{6y^{2n}}{2y^n} - \frac{4ay^{n+1}}{2y^n} = 3y^{2n-n} - 2ay^{n+1-n} \\ = 3y^n - 2ay$$

$$24. \frac{3a(F+T)b^2 - (F+T)}{a(F+T)} = \frac{3a(F+T)b^2}{a(F+T)} - \frac{(F+T)}{a(F+T)} \\ = 3b^2 - \frac{1}{a}$$

$$25. x + 3 \overline{)2x^2 + 7x + 3}$$

$$\begin{array}{r} 2x + 1 \\ 2x^2 + 6x \\ \hline x + 3 \end{array}$$

$$26. t - 1 \overline{)3t^2 - 7t + 4}$$

$$\begin{array}{r} 3t - 4 \\ 3t^2 - 3t \\ \hline - 4t + 4 \\ \begin{array}{r} t + 3 \\ 0 \end{array} \end{array}$$

$$\begin{array}{r} x-1 \\ \hline 27. \quad x-2 \overline{)x^2 - 3x + 2} \\ \underline{x^2 - 2x} \\ -x+2 \\ -x+2 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 2x-7 \\ \hline 28. \quad x+1 \overline{)2x^2 - 5x - 7} \\ \underline{2x^2 + 2x} \\ -7x-7 \\ -7x-7 \\ \hline 0 \end{array}$$

$$\begin{array}{r} x^2 + x - 6 \\ \hline 33. \quad x+2 \overline{x^3 + 3x^2 - 4x - 12} \\ \underline{x^3 + 2x^2} \\ x^2 - 4x \\ \underline{x^2 + 2x} \\ -6x - 12 \\ -6x - 12 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 4x^2 - x - 1 \\ \hline 29. \quad 2x-3 \overline{)8x^3 - 14x^2 + x + 0} \\ \underline{8x^3 - 12x^2} \\ -2x^2 + x \\ -2x^2 + 3x \\ \hline -2x + 0 \\ -2x + 3 \\ \hline -3 \end{array}$$

$$\begin{array}{r} x^2 + 7x + 9 \\ \hline 34. \quad 3x-2 \overline{)3x^3 + 19x^2 + 13x - 20} \\ \underline{3x^3 - 2x^2} \\ 21x^2 + 13x \\ \underline{21x^2 - 14x} \\ 27x - 20 \\ \hline 27x - 18 \\ -2 \end{array}$$

$$\begin{array}{r} 3y+2 \\ \hline 30. \quad 2y+1 \overline{)6y^2 + 7y + 6} \\ \underline{6y^2 + 3y} \\ 4y + 6 \\ \underline{4y + 2} \\ 4 \end{array}$$

$$\frac{3x^3 - 19x^2 + 13x - 20}{3x - 2} = x^2 + 7x + 9 - \frac{2}{3x - 2}$$

$$(6 + 7y + 6y^2) \div (2y + 1) = 3y + 2 + \frac{4}{2y + 1}$$

$$\begin{array}{r} 2a^2 + 8 \\ \hline 35. \quad a^2 - 2 \overline{)2a^4 + 0a^3 + 4a^2 + 0a - 16} \\ \underline{2a^4} \quad \underline{-4a^2} \\ +8a^2 \quad -16 \\ \underline{8a^2} \quad \underline{-16} \\ 0 \end{array}$$

$$\frac{2a^4 + 4a^2 - 16}{a^2 - 2} = 2a^2 + 8 + \frac{0}{a^2 - 2}$$

$$\begin{array}{r} Z-2 \\ \hline 31. \quad 4Z+3 \overline{)4Z^2 - 5Z - 7} \\ \underline{4Z^2 + 3Z} \\ -8Z - 7 \\ \underline{-8Z - 6} \\ -1 \end{array}$$

$$\begin{array}{r} 2T+1 \\ \hline 36. \quad 3T^2 - T + 2 \overline{)6T^3 + T^2 + 0T + 2} \\ \underline{6T^3 - 2T^2 + 4T} \\ 3T^2 - 4T + 2 \\ \underline{3T^2 - T + 2} \\ -3T \end{array}$$

$$(4Z^2 - 5Z - 7) \div (4Z + 3) = Z - 2 + \frac{-1}{4Z + 3}$$

$$\frac{6T^3 + T^2 + 2}{3T^2 - T + 2} = 2T + 1 + \frac{-3T}{3T^2 - T + 2}$$

$$\begin{array}{r} 2x+1 \\ \hline 32. \quad 3x-4 \overline{)6x^2 - 5x - 9} \\ \underline{6x^2 - 8x} \\ 3x - 9 \\ \underline{3x - 4} \\ -5 \end{array}$$

$$(6x^2 - 5x - 9) \div (3x - 4) = 2x + 1 + \frac{-5}{3x - 4}$$

$$37. \quad x+2 \overline{)x^3 + 0x^2 + 0x + 8} \\ \underline{x^3 + 2x^2} \\ -2x^2 + 0x \\ \underline{-2x^2 - 4x} \\ 4x + 8 \\ \underline{4x + 8} \\ 0$$

$$38. \quad D-1 \overline{)D^3 + 0D^2 + 0D - 1} \\ \underline{D^3 - D^2} \\ D^2 + 0D \\ \underline{D^2 - D} \\ D-1 \\ \underline{D-1} \\ 0$$

$$39. \quad x-y \overline{)x^2 - 2xy + y^2} \\ \underline{x^2 - xy} \\ -xy + y^2 \\ \underline{-xy + y^2} \\ 0$$

$$40. \quad r-3R \overline{)3r^2 - 5rR + 2R^2} \\ \underline{3r^2 - 9rR} \\ 4rR + 2R^2 \\ \underline{4rR - 12R^2} \\ 14R^2$$

$$41. \quad x+y-z \overline{)x^2 + 0xy + 0xz - y^2 + 2yz - z^2} \\ \underline{x^2 + xy - xz} \\ -xy + xz - y^2 + 2yz - z^2 \\ \underline{-xy - y^2 + yz} \\ +xz + yz - z^2 \\ \underline{+xz + yz - z^2} \\ 0$$

$$\frac{x^2 - y^2 + 2yz - z^2}{x+y-z} = x - y + z + \frac{0}{x+y-z}$$

$$42. \quad a^2 - 2ab + 2b^2 \overline{)a^4} \\ \underline{a^4 - 2a^3b + 2a^2b^2} \\ + 2a^3b - 2a^2b^2 \\ \underline{+ 2a^3b - 4a^2b^2 + 4ab^3} \\ + 2a^2b^2 - 4ab^3 \\ \underline{+ 2a^2b^2 - 4ab^3 + 4b^4} \\ - 3b^4 \\ \frac{a^4 + b^4}{a^2 - 2ab + 2b^2} = (a^2 + 2ab + 2b^2) + \frac{-3b^4}{a^2 - 2ab + 2b^2}$$

$$43. \quad x+c \overline{)2x^2 - 9x - 5} \\ \underline{2x^2 + 2cx} \\ (-9-2c)x - 5 \\ \underline{(-9-2c)x + c(-9-2c)} \\ -5 - c(-9-2c)$$

The required value of c must make $(-9-2c)=1 \Rightarrow$

$c=-5$ and must make $-5 - c(-9-2c)=0$.

$$-5 - c(-9-2c)=0 \Rightarrow 2c^2 + 9c - 5 = 0$$

$$(2c-1)(c+5)=0$$

$$2c-1=0 \quad c+5=0$$

$$c=\frac{1}{2}, \quad c=-5$$

$c=-5$ is the required value.

$$44. \quad 3x+4 \overline{)6x^2 - x + k} \\ \underline{6x^2 + 18x} \\ -9x + k \\ \underline{-9x - 12} \\ k + 12$$

$$k + 12 = 0$$

$$k = -12$$

$$45. \begin{array}{r} x^3 - x^2 + x - 1 \\ x+1 \overline{)x^4} & +1 \\ x^4 + x^3 \\ \hline -x^3 \\ \hline -x^3 - x^2 \\ \hline x^2 \end{array}$$

$$\begin{array}{r} x^2 + x \\ -x+1 \\ \hline -x - 1 \\ \hline 2 \end{array}$$

$$\frac{x^4 + 1}{x+1} = x^3 - x^2 + x - 1 + \frac{2}{x+1} \neq x^3$$

$$46. \begin{array}{r} x^2 - xy + y^2 \\ x+y \overline{)x^3} & + y^3 \\ x^3 + x^2 y \\ \hline -x^2 y \\ \hline -x^2 y - xy^2 \\ \hline xy^2 + y^3 \\ \hline xy^2 + y^3 \\ \hline 0 \end{array}$$

$$\frac{x^3 + y^3}{x+y} = x^2 - xy + y^2 \neq x^2 + y^2$$

$$47. \begin{array}{r} 2x^2 + x - 4 \\ 3x-2 \overline{)6x^3 - x^2 - 14x + k} \\ 6x^3 - 4x^2 \\ \hline 3x^2 - 14x \\ 3x^2 - 2x \\ \hline -12x + k \\ -12x + 8 \\ \hline k - 8 \end{array}$$

$$k - 8 = -2$$

$$k = 6$$

$$48. \begin{array}{r} 3x+2 \\ 2x+5 \overline{)6x^2 + 19x + 10} \\ 6x^2 + 15x \\ \hline 4x + 10 \\ 4x + 10 \\ \hline 0 \end{array}$$

The width is $3x + 2$.

$$49. \begin{aligned} & \frac{8A^5 + 4A^3\mu^2E^2 - A\mu^4E^4}{8A^4} \\ &= \frac{8A^5}{8A^4} + \frac{4A^3\mu^2E^2}{8A^4} - \frac{A\mu^4E^4}{8A^4} \\ &= A + \frac{\mu^2E^2}{2A} - \frac{\mu^4E^4}{8A^3} \end{aligned}$$

$$50. \begin{aligned} & \frac{6R_1 + 6R_2 + R_1R_2}{6R_1R_2} = \frac{6R_1}{6R_1R_2} + \frac{6R_2}{6R_1R_2} + \frac{R_1R_2}{6R_1R_2} \\ &= \frac{1}{R_2} + \frac{1}{R_1} + \frac{1}{6} \end{aligned}$$

$$51. \begin{aligned} & \frac{GMm[(R+r)-(R-r)]}{2rR} = \frac{GMm[R+r-R+r]}{2rR} \\ &= \frac{GMm[2r]}{2rR} = \frac{GMm}{R} \end{aligned}$$

$$52. \begin{array}{r} 3T^2 - 2T - 4 \\ T-2 \overline{)3T^3 - 8T^2 + 0T + 8} \\ 3T^3 - 6T^2 \\ \hline -2T^2 \\ -2T^2 + 4T \\ \hline -4T + 8 \\ -4T + 8 \\ \hline 0 \end{array}$$

$$53. \left(\frac{s^2 - 2s - 2}{s^4 + 4} \right)^{-1} = \frac{s^4 + 4}{s^2 - 2s - 2}$$

$$\begin{array}{r} s^2 + 2s + 6 \\ s^2 - 2s - 2 \overline{)s^4 + 0s^3 + 0s^2 + 0s + 4} \\ s^4 - 2s^3 - 2s^2 \\ \hline 2s^3 + 2s^2 + 0s \\ 2s^3 - 4s^2 - 4s \\ \hline 6s^2 + 4s + 4 \\ 6s^2 - 12s - 12 \\ \hline 16s + 16 \end{array}$$

54.
$$\begin{array}{r} t^2 - 3t + 5 \\ \overline{2t+100)2t^3 + 94t^2 - 290t + 500} \\ 2t^3 + 100t^2 \\ \hline -6t^2 - 290t \\ -6t^2 - 300t \\ \hline 10t + 500 \\ \hline 10t + 500 \\ \hline 0 \end{array}$$

1.10 Solving Equations

1. (a) $x - 3 = -12$

$$x - 3 + 3 = -12 + 3$$

$$x = -9$$

(b) $x + 3 = -12$

$$x + 3 - 3 = -12 - 3$$

$$x = -15$$

(c) $\frac{x}{3} = -12$

$$3\left(\frac{x}{3}\right) = 3(-12)$$

$$x = -36$$

(d) $3x = -12$

$$\frac{3x}{3} = \frac{-12}{3}$$

$$x = -4$$

2. $7 - 2t = 9$

$$\begin{aligned} -2t &= 9 - 7 \\ -2t &= 2 \\ t &= -1 \end{aligned}$$

Check:

$$\begin{aligned} 7 - (2)(-1) &\stackrel{?}{=} 9 \\ 7 - (-2) &\stackrel{?}{=} 9 \\ 7 + 2 &\stackrel{?}{=} 9 \\ 9 &= 9 \end{aligned}$$

3. $x - 7 = 3x - (8 - 6x)$

$$\begin{aligned} x - 7 &= 3x - 8 + 6x \\ x - 7 &= 9x - 8 \\ -8x &= -1 \\ x &= \frac{1}{8} \end{aligned}$$

4. $\frac{L}{3.80} = \frac{7}{4}$

$$L = 3.80\left(\frac{7}{4}\right)$$

$$L = 6.65$$

5. $x - 2 = 7$

$$\begin{aligned} x &= 7 + 2 \\ x &= 9 \end{aligned}$$

7. $x + 5 = 4$

$$\begin{aligned} x &= 4 - 5 \\ x &= -1 \end{aligned}$$

9. $\frac{t}{2} = -5$

$$\begin{aligned} t &= 2(-5) \\ t &= -10 \end{aligned}$$

6. $x - 4 = -1$

$$x = 3$$

8. $s + 6 = -3$

$$s = -9$$

10. $\frac{x}{-4} = 2$

$$\begin{aligned} x &= (-4)(2) \\ x &= -8 \end{aligned}$$

11. $4E = -20$

$$E = \frac{-20}{4} = -5$$

12. $2x = 12$

$$x = 6$$

13. $3t + 5 = -4$

$$\begin{aligned} 3t &= -4 - 5 \\ 3t &= -9 \\ t &= -3 \end{aligned}$$

14. $5D - 2 = 13$

$$5D = 15$$

15. $5 - 2y = -3$

$$\begin{aligned} -2y &= -3 - 5 \\ y &= \frac{-8}{-2} = 4 \end{aligned}$$

16. $-5t + 8 = 18$

$$\begin{aligned} -5t &= 18 - 8 \\ t &= -2 \end{aligned}$$

17. $3x + 7 = x$

$$\begin{aligned} 3x - x &= -7 \\ 2x &= -7 \\ x &= \frac{-7}{2} \end{aligned}$$

18. $6 + 4L = 5 - 3L$

$$\begin{aligned} 7L &= -1 \\ L &= \frac{-1}{7} \end{aligned}$$

19. $2(s - 4) = s$

$$\begin{aligned} 2s - 8 &= s \\ s - 8 &= 0 \\ s &= 8 \end{aligned}$$

20. $3(4 - n) = -n$

$$\begin{aligned} 12 - 3n &= -n \\ -2n &= -12 \\ n &= 6 \end{aligned}$$

21. $-(r - 4) = 6 + 2r$

$$\begin{aligned} -r + 4 &= 6 + 2r \\ -3r &= 2 \\ r &= \frac{-2}{3} \end{aligned}$$

22. $-(x + 2) + 5 = 5x$

$$\begin{aligned} 5 - x - 2 &= 5x \\ -6x &= -3 \\ x &= \frac{1}{2} \end{aligned}$$

23. $2(x-3) = -x$
 $2x-6 = -x$
 $2x+x = 6$
 $3x = 6$
 $x = 2$

24. $4(7-F) = -7$
 $28-4F = -7$
 $-4F = -35$
 $F = \frac{35}{4}$

30. $2x = \frac{-5(7-3x)+3}{4}$
 $8x = 3 - 5(7-3x)$
 $8x = 3 - 35 + 15x$
 $-7x = -32$
 $x = \frac{32}{7}$

25. $0.1x - 0.5(x-2) = 2$
 $x - 5(x-2) = 20$
 $x - 5x + 10 = 20$
 $-4x = 10$
 $x = -2.5$

31. $|x| - 1 = 8$
 $|x| = 9$
 $x = -9 \text{ or } x = 9$

32. $2 - |x| = 4$
 $-|x| = 2$
 $|x| = -2, \text{ no solution}$

26. $1.5x - 0.3(x-4) = 6$
 $15x - 3(x-4) = 60$
 $15x - 3x + 12 = 60$
 $12x = 48$
 $x = 4$

33. $|2x-3| = 5$
 $2x-3 = 5 \text{ or } 2x-3 = -5$
 $2x = 8 \quad 2x = -2$
 $x = 4 \quad x = -1$

27. $-4 - 3(1-2p) = -7 + 2p$
 $7 - 3 + 6p = 4 + 2p$
 $6p - 2p = 4 - 7 + 3$
 $4p = 0$
 $p = \frac{0}{4} = 0$

34. $|7-x| = 1$
 $7-x = 1 \text{ or } 7-x = -1$
 $x = 6 \quad x = 8$

28. $3 - 6(2-3t) = t - 5$
 $3 - 12 + 18t = t - 5$
 $17t = 4$
 $t = \frac{4}{17}$

35. $5.8 - 0.3(x-6.0) = 0.5x$
 $5.8 - 0.3x + 1.8 = 0.5x$
 $7.6 = 0.8x$
 $x = 9.5$

29. $\frac{4x-2(x-4)}{3} = 8$
 $4x-2(x-4) = 24$
 $4x-2x+8 = 24$
 $2x = 16$
 $x = 8$

36. $1.9t = 0.5(4.0-t) - 0.8$
 $1.9t = 2.0 - 0.5t - 0.8$
 $2.4t = 1.2$
 $t = 0.5$

37. $-0.24(C-0.50) = 0.63$
 $-0.24C + 0.12 = 0.63$
 $-0.24C = 0.63 - 0.12$
 $-0.24C = 0.51$
 $C = -2.1$

38. $27.5(5.17 - 1.44x) = 73.4$
 $142.2 - 39.6x = 73.4$
 $-39.6x = -68.8$
 $x = 1.74$

39. $\frac{x}{2.0} = \frac{17}{6.0}$
 $x = \frac{34}{6.0}$
 $x = 5.7$

40. $\frac{3.0}{7.0} = \frac{x}{42}$
 $\frac{126}{7.0} = x$
 $x = 18$

41. $\frac{165}{223} = \frac{13V}{15}$
 $\frac{15}{13} \left(\frac{165}{223} \right) = \frac{15}{13} \left(\frac{13V}{15} \right)$
 $V = \frac{2475}{2899} = 0.85$

42. $\frac{276x}{17.0} = \frac{1360}{46.4}$
 $x = \frac{1360}{46.4} \cdot \frac{17.0}{276}$
 $x = 1.81$

43. (a) $2x + 3 = 3 + 2x$
 $2x + 3 = 2x + 3$, identity

(b) $2x - 3 = 3 - 2x$
 $2x - 3 + 3 = 3 + 3 - 2x$
 $2x = 6 - 2x$
 $4x = 6$
 $x = \frac{3}{2}$, conditional

44. For $a = 0$, $2x + a = 2x$ because $2x + 0 = 2x$
 $2x = 2x$

an identity. For $a \neq 0$, $2x + a = 2x$
 $a = 2x - 2x$
 $a = 0$ but $a \neq 0$
 $\Rightarrow 2x + a = 2x$ is a contradiction for $a \neq 0$.

Thus, for all values of a ($a = 0$ or $a \neq 0$) $2x + a = 2x$ is either an identity or a contradiction. So there are no values for a for which $2x + a = 2x$ is a conditional equation.

45. EQUATION SOLVER
 $\text{eqn: } 0 = x - 7 - 3x + (6x - 8)$

$x - 7 - 3x + (6x - 8) = 0$
 $x = 3.75$
 $\text{bound} = [-1e99, 1...]$

3.75 • Frac 15/4

46. EQUATION SOLVER
 $\text{eqn: } 0 = 0.0595 - 0.525x$
 $25x - 8.85(x + 0.003)$
 16

0.0595 - 0.525x = 0
 $x = .00336362666$ ■
 $\text{bound} = [-1e99, 1...]$

47. $0.03x + 0.06(2000 - x) = 96$

$$\begin{aligned} 0.03x + 120 - 0.06x &= 96 \\ -0.03x &= -24 \\ x &= 800 \end{aligned}$$

48. $15(5.5 + v) = 24(5.5 - v)$

$$\begin{aligned} 82.5 + 15v &= 132 - 24v \\ 39v &= 49.5 \\ v &= 1.3 \text{ km/h} \end{aligned}$$

49. $1.1 = \frac{T - 76}{40}$
 $44 = T - 76$
 $T = 120^\circ\text{C}$

50. $1.12V - 0.67(10.5 - V) = 0$

$$1.12V - 7.035 + 0.67V = 0$$

$$1.79V = 7.035$$

$$V = 3.9V$$

51. $0.14n + 0.06(2000 - n) = 0.09(2000)$

$$0.14n + 120 - 0.06n = 180$$

$$0.08n = 180 - 120$$

$$n = 750 \text{ gal}$$

52. $210(3x) = 55.3x + 38.5(8.25 - 3x)$

$$630x = 55.3x + 317.625 - 115.5x$$

$$690.2x = 317.625$$

$$x = 0.46 \text{ m}$$

53. $\frac{x}{5.5} = \frac{1250}{15}$

$$x = \frac{1250(5.5)}{15}$$

$$x = 460 \text{ mi}$$

54. $\frac{1.8}{20} = \frac{x}{16}$

$$x = \frac{1.8(16)}{20}$$

$$x = 1.4 \text{ m}$$

3. $V = V_{\circ} [1 + b(T - T_{\circ})]$

$$V = V_{\circ} [1 + bT - bT_{\circ}]$$

$$V = V_{\circ} + bV_{\circ}T - bV_{\circ}T_{\circ}$$

$$bV_{\circ}T_{\circ} = V_{\circ} + bV_{\circ}T - V$$

$$T_{\circ} = \frac{V_{\circ} + bV_{\circ}T - V}{bV_{\circ}}$$

4. $R = R_{\circ} + R_{\circ}\alpha T$

$$R_{\circ}\alpha T = R - R_{\circ}$$

$$\alpha = \frac{R - R_{\circ}}{R_{\circ}T}$$

5. $E = IR$

$$\frac{E}{I} = \frac{IR}{I}$$

$$R = \frac{E}{I}$$

6. $PV = nRT$

$$T = \frac{PV}{nR}$$

7. $rL = g_2 - g_1$

$$g_1 = g_2 - rL$$

8. $W = S_d T - Q$

$$Q = S_d T - W$$

9. $Q = SLd^2$

$$L = \frac{Q}{Sd^2}$$

10. $P = 2\pi Tf$

$$T = \frac{P}{2\pi f}$$

11. $p = p_a + dgh$

$$p - p_a = dgh$$

$$\frac{p - p_a}{dh} = \frac{dgh}{dh}$$

$$g = \frac{p - p_a}{dh}$$

12. $2Q = 2I + A + S$

$$\frac{2Q - A - S}{2} = I$$

1.11 Formulas and Literal Equations

1. $v - v_{\circ} = at$

$$a = \frac{v - v_{\circ}}{t}$$

2. $W = \frac{L(wL + 2P)}{8}$

$$8W = L(wL + 2P)$$

$$8W = L^2w + 2LP$$

$$L^2w = 8W - 2LP$$

$$w = \frac{8W - 2LP}{L^2}$$

$$\begin{aligned} \text{13. } A &= \frac{Rt}{PV} \\ Rt &= APV \\ V &= \frac{Rt}{AP} \end{aligned}$$

$$\text{15. } ct^2 = 0.3t - ac$$

$$\begin{aligned} ac &= 0.3t - ct^2 \\ a &= \frac{0.3t - ct^2}{c} \end{aligned}$$

$$\text{16. } 2p + dv^2 = 2d(C - W)$$

$$2p + dv^2 = 2dC - 2dW$$

$$\begin{aligned} 2dC &= 2p + dv^2 + 2dW \\ C &= \frac{2p + dv^2 + 2dW}{2d} \end{aligned}$$

$$\text{17. } T = \frac{c+d}{v}$$

$$\begin{aligned} Tv &= c+d \\ d &= Tv - c \end{aligned}$$

$$\text{19. } \frac{K_1}{K_2} = \frac{m_1 + m_2}{m_1}$$

$$K_1 m_1 = K_2 m_1 + K_2 m_2$$

$$K_2 m_2 = K_1 m_1 - K_2 m_1$$

$$m_2 = \frac{K_1 m_1 - K_2 m_1}{K_2}$$

$$\text{20. } f = \frac{F}{d-F}$$

$$fd - fF = F$$

$$fd = F + fF$$

$$d = \frac{F + fF}{f}$$

$$\text{21. } a = \frac{2mg}{M+2m}$$

$$aM + 2ma = 2mg$$

$$aM = 2mg - 2ma$$

$$M = \frac{2mg - 2ma}{a}$$

$$\text{31. } N = N_1 T - N_2 (1-T)$$

$$N + N_2 (1-T) = N_1 T$$

$$N_1 = \frac{N + N_2 - N_2 T}{T}$$

$$\begin{aligned} \text{14. } u &= -\frac{eL}{2u} \\ L &= -\frac{2um}{e} \end{aligned}$$

$$\begin{aligned} \text{22. } v &= \frac{V(m+M)}{m} \\ mv &= Vm + VM \\ VM &= mv - mV \\ M &= \frac{mv - mV}{V} \end{aligned}$$

$$\begin{aligned} \text{23. } C_0^2 &= C_1^2 (1+2V) \\ C_0^2 &= C_1^2 + 2C_1^2 V \\ V &= \frac{C_0^2 - C_1^2}{2C_1^2} \end{aligned}$$

$$\text{24. } A_l = A(M+1)$$

$$A_l = AM + A$$

$$M = \frac{A_l - A}{A}$$

$$\text{25. } N = r(A-s)$$

$$N = rA - rs$$

$$rs = rA - N$$

$$s = \frac{rA - N}{r}$$

$$\text{26. } T = 3(T_2 - T_1)$$

$$T = 3T_2 - 3T_1$$

$$T_1 = \frac{3T_2 - T}{3}$$

$$\text{27. } T_2 = T_1 - \frac{h}{100}$$

$$\frac{h}{100} = T_1 - T_2$$

$$h = 100(T_1 - T_2)$$

$$\text{28. } p_2 = p_1 + rp_1(1-p_1)$$

$$p_2 - p_1 = rp_1(1-p_1)$$

$$r = \frac{p_2 - p_1}{p_1(1-p_1)}$$

$$\text{29. } Q_l = P(Q_2 - Q_l)$$

$$Q_l = PQ_2 - PQ_l$$

$$Q_l(1+P) = PQ_2$$

$$Q_2 = \frac{Q_l + PQ_l}{P}$$

$$\text{30. } p - p_a = dg(y_2 - y_1)$$

$$y_2 - y_1 = \frac{p - p_a}{dg}$$

$$y_1 = y_2 - \frac{p - p_a}{dg}$$

$$\text{32. } t_a = t_c + (1-h)t_m$$

$$\frac{t_a - t_c}{t_m} = 1 - h$$

$$h = 1 - \frac{t_a - t_c}{t_m}$$

33. $L = \pi(r_1 + r_2) + 2x_1 + x_2$
 $L = \pi r_1 + \pi r_2 + 2x_1 + x_2$
 $\pi r_1 = L - \pi r_2 - 2x_1 - x_2$
 $r_1 = \frac{L - \pi r_2 - 2x_1 - x_2}{\pi}$

34. $I = \frac{VR_2 + VR_1(1+\mu)}{R_1 R_2}$

$$\frac{IR_1 R_2 - VR_2}{VR_1} = 1 + \mu$$

$$\mu = \frac{IR_1 R_2 - VR_2}{VR_1} - 1$$

35. $P = \frac{V_1(V_2 - V_1)}{gJ}$

$$gJP = V_1 V_2 - V_1^2$$

$$gJP + V_1^2 = V_1 V_2$$

$$V_2 = \frac{gJP + V_1^2}{V_1}$$

36. $W = T(S_1 - S_2) - Q$

$$\frac{W + Q}{T} = S_1 - S_2$$

$$S_2 = S_1 - \frac{W + Q}{T}$$

37. $C = \frac{2eAk_1k_2}{d(k_1 + k_2)}$

$$Cd(k_1 + k_2) = 2eAk_1k_2$$

$$e = \frac{Cd(k_1 + k_2)}{2Ak_1k_2}$$

38. $d = \frac{3LPx^2 - Px^3}{GEI}$

$$GEId = 3LPx^2 - Px^3$$

$$3LPx^2 = GEId + Px^3$$

$$L = \frac{GEId + Px^3}{3Px^2}$$

39. $V = C\left(1 - \frac{n}{N}\right)$

$$V = C - \frac{C}{N} \cdot n$$

$$\frac{C}{N} \cdot n = C - V$$

$$n = \frac{N}{C}(C - V) = N - \frac{NV}{C}$$

40. $\frac{p}{P} = \frac{AI}{B + AI}$

$$p(B + AI) = PAI$$

$$pB + pAI = PAI$$

$$pB = PAI - pAI$$

$$B = \frac{PAI - pAI}{p}$$

41. $p(C - n) + n = A$

$$pC - pn + n = A$$

$$n = \frac{A - pC}{1 - p}$$

$$n = \frac{13.0 - 0.25(15.0)}{1 - 0.25}$$

$$n = 12 \text{ L}$$

42. $P_t = P_c(1 + 0.500m^2)$

$$P_c = \frac{P_t}{1 + 0.500m^2} = \frac{680}{1 + 0.500(0.925)^2}$$

$$P_c = 476 \text{ W}$$

43. $F = \frac{9}{5}C + 32$

$$90.2 = \frac{9}{5}C + 32$$

$$\frac{5}{9}(90.2 - 32) = C$$

$$C = \frac{5}{9} \times 58.2$$

$$C = 32.3^\circ\text{C}$$

44. $V = \frac{1}{2}L(B + b)$

$$b = \frac{2V}{L} - B = \frac{2(38.6)}{16.1} - 2.63$$

$$b = 2.17 \text{ ft}^2$$

45. $V_1 = \frac{VR_1}{R_1 + R_2}$

$$R_1 + R_2 = \frac{VR_1}{V_1}$$

$$R_2 = \frac{VR_1}{V_1} - R_1 = \frac{12.0(3.56)}{6.30} - 3.56$$

$$R_2 = 3.22\Omega$$

46. $E = \frac{1}{q + p(1-q)}$

$$qE + Ep(1-q) = 1$$

$$Ep(1-q) = 1 - qE$$

$$p = \frac{1 - qE}{E(1-q)} = \frac{1 - 0.83(0.66)}{0.66(1 - 0.83)}$$

$$p = 4$$

47. $d = v_2 \cdot 4 + v_1(t+2)$

$$d = 4v_2 + v_1t + 2v_1$$

$$v_1t = d - 4v_2 - 2v_1$$

$$t = \frac{d - 4v_2 - 2v_1}{v_1} \text{ h}$$

48. $x + 15y = C$

$$15y = C - x$$

$$y = \frac{C - x}{15}$$

1.12 Applied Word Problems

1. $x = \text{number of } 25 \text{ W lights}$

$$37 - x = \text{number of } 40 \text{ W lights}$$

$$25x + 40(37 - x) = 1000$$

$$25x + 1480 - 40x = 1000$$

$$-15x = -480$$

$$x = 32, \text{ } 25 \text{ W lights}$$

$$37 - x = 5, \text{ } 40 \text{ W lights}$$

2. $x = \text{number of slides with } 5 \text{ mg}$

$$x - 3 = \text{number of slides with } 6 \text{ mg}$$

$$5x = 6(x - 3)$$

$$5x = 6x - 18$$

$$-x = -18$$

$$x = 18$$

$$18 \text{ slides with } 5 \text{ mg}$$

3. $29,500t = 6000 + 27,500t$

$$2000t = 6000$$

$$t = 3.000 \text{ h}$$

4. $0.0500(7600) + 0.500x = 0.100(7600 + x)$

$$380 + 0.500x = 760 + 0.100x$$

$$0.400x = 380$$

$$x = 950 \text{ L}$$

5. $x = \text{cost 6 years ago}$

$$x + 5000 = \text{cost today}$$

$$x + (x + 5000) = 64,000$$

$$2x + 5000 = 64,000$$

$$2x = 59,000$$

$$x = 29,500$$

$$x + 5000 = 34,500$$

\$29,500 six years ago \$34,500 is the cost today

6. Let x = flow rate of first stream in ft^3/s ;

$$x + 1700 = \text{flow rate of second stream in } \text{ft}^3/\text{s}$$

$$(x + x + 1700) \cdot 3600 = 1.98 \times 10^7$$

$$x = 1900 \text{ ft}^3/\text{s}$$

$$x + 1700 = 3600 \text{ ft}^3/\text{s}$$

7. Let x = recycled cars the first year;

$$x + 500,000 = \text{recycled cars the second year}$$

$$x + x + 500,000 = 6.9 \times 10^6$$

$$2x = 6,400,000$$

$$x = 3.2 \text{ million the first year;}$$

$$3.7 \text{ million the second year}$$

8. Let x = number of times accessed on 1st day

$$\frac{x}{4} + 40,000 = \text{number of times accessed on 2nd day}$$

$$\frac{x}{4} = \text{number of times accessed on 3rd day}$$

$$x = \frac{x}{4} + 40,000 + \frac{x}{4} \text{ from which}$$

$$x = 80,000, \text{ 1st day}$$

$$\frac{x}{4} + 40,000 = 60,000, \text{ 2nd day}$$

$$\frac{x}{4} = 20,000, \text{ 3rd day}$$

9. Let x = number of acres @ \$200

$$200 \cdot x + 300 \cdot (140 - x) = 37,000$$

$$2x + 420 - 3x = 370$$

$$x = 50 \text{ acres @ \$200}$$

$$140 - x = 90 \text{ acres @ \$300}$$

10. Let x = mg in first dose

$$x + 660 = \text{mg in second dose}$$

$$x + x + 660 = 2000$$

$$x = 670 \text{ mg in first dose}$$

$$x + 660 = 1330 \text{ mg in second dose}$$

11. x = amount after ppm/h

$$5x = 3(150)$$

$$x = 90$$

$$150 - 90 = 60 \text{ ppm/h reduction}$$

12. Let x = number of teeth in 1st gear

$$x + 13 = \text{number of teeth in 2nd gear}$$

$$(x + 13) + 15 = x + 28 = \text{number of teeth in 3rd gear}$$

$$x + x + 13 + x + 28 = 107$$

$$3x + 41 = 107$$

$$3x = 66$$

$$x = 22$$

$$x + 13 = 35$$

$$x + 28 = 50$$

The three gears have 22, 35, and 50 teeth.

13. Let $x = 15 \text{ m girders}$

$$x - 4 = 18 \text{ m girders}$$

$$15x = 18(x - 4)$$

$$3x = 72$$

$$x = 24,$$

so there are twenty 18 m girders needed, from

which $L = 20(18) = 360 \text{ m}$ for span.

14. Let x = number of gal used per week to use up original supply in eight weeks.

$$8x = 6(x + 5000) \text{ from which}$$

$$x = 15,000$$

$$8x = 120,000 \text{ gal in original supply}$$

15. $x + 2x + (x + 9.2) = 0$

$$4x = -9.2 \Rightarrow x = -2.3 \mu\text{A} \text{ for the first current}$$

$$2x = -4.6 \mu\text{A} \text{ for the second current}$$

$$x + 9.2 = 6.9 \mu\text{A} \text{ for the third current}$$

16. Let x = number of trucks in first fleet

$$x + 5 = \text{number of trucks in second fleet}$$

$$8x + 6(x + 5) = 198 \text{ from which}$$

$$x = 12 \text{ trucks in first fleet}$$

$$x + 5 = 17 \text{ trucks in second fleet}$$

17. Let x = the main pipeline

$$x + 2.6 = \text{the smaller pipeline}$$

$$3(x + 2.6) + x = 35.4$$

$$3x + 7.8 + x = 35.4$$

$$4x = 27.6$$

$$x = 6.9 \text{ km for the main pipeline;}$$

$$9.5 \text{ km for the smaller pipeline}$$

18. $G_1 + G_2 = 750 \Rightarrow G_2 = 750 - G_1$
 $0.65G_1 + 0.75G_2 = 530$
 $0.65G_1 + 0.75(750 - G_1) = 530$
 $0.65G_1 + 562.5 - 0.75G_1 = 530$
 $-0.10G_1 = -32.5$
 $G_1 = 325 \text{ MW}$
 $G_2 = 750 - G_1 = 425 \text{ MW}$

19. $E = 2D, P = D + 75,$
 $40E + 80P + 140D = 42,000$
 $40(2D) + 80(D + 75) + 140D = 42,000$
 $300D = 36,000$
 $d = 120$
 $E = 2D = 240$
 $P = D + 75 = 195$

20. $0.75(20,000) = 15,000 \text{ after taxes}$
 $x + y = 15,000 \Rightarrow y = 15,000 - x$
 $0.40x - 0.10y = 2000$
 $0.40x - 0.10(15,000 - x) = 2000$
 $0.4x - 1500 + 0.1x = 2000$
 $0.5x = 3500$
 $x = \$7000 \text{ at 40\% gain}$
 $y = 15,000 - x = \$8000 \text{ at 10\% gain}$

21. To completely pass each other, the rear of the 520 ft train must travel $(520 + 440)$ ft at a relative speed of 100 mph, from which
 $(520 + 440) \text{ ft} \cdot \left(\frac{\text{mi}}{5280 \text{ ft}}\right) = 100 \frac{\text{mi}}{\text{h}} \cdot t$
 $t = 0.0018 \text{ h} = 6.54 \text{ s}$

22. $I - P = 3850$
 $P = 0.23I \Rightarrow I = \frac{P}{0.23}$
 $\frac{P}{0.23} - P = 3850$
 $P = \$1150$

23. Let $d = \text{slope length}$
 $d = vt, t = \frac{d}{v}, \frac{d}{v_1} = 24 = \frac{d}{v_2}$
 $\frac{d}{50} = 24 - \frac{d}{140}; \frac{d}{50} + \frac{d}{150} = 24$
 $0.0267d = 24; d = 900 \text{ m}$

24. Let $x = \text{speed of sound}$
 $(x - 120)(1.0) + (x + 410)(3.0) = 3990 \text{ from which}$
 $x = 720 \text{ mi/h,}$
 speed of sound

25. Let $v = \text{speed of French train}$
 $v\left(\frac{17}{60}\right) + (v - 8)\left(\frac{17}{60}\right) = 50 \Rightarrow 17v + 17v - 136$
 $3000 \Rightarrow 34v = 3136 \Rightarrow v = 92.2$
 $v - 8 = 84.2$

The speed of the French train is 92.2 km/h. The speed of the English train is 84.2 km/h.

26. Let $t = \text{time until appointment}$
 $60.0(t - 10) = 45.0(t - 5.0) \text{ from which}$
 $t = 25 \text{ min until the appointment}$

27. Let $x - 30 = \text{time first car started race};$
 $x = \text{time second car started race}$
 $260(x - 30) = 240(x)$
 $260x - 7800 = 240x$
 $20x = 7800$
 $x = 390 \text{ s}$
 $8 \text{ laps} = 250 \times 8 = 20 \text{ mi}, 105,600 \text{ ft, total distance}$
 $d = vt = 260 \times 390 = 101,400 \text{ ft} < 105,600 \text{ ft}$
So, the first car is ahead after 8 laps.

28. Let $x = \# \text{ of 1st type, tested 0.5\% defective}$
 $6100 - x = \# \text{ of 2nd type tested, 0.8\% defective}$
 $0.005x + 0.008(6100 - x) = 38 \text{ from which}$
 $x = 3600 \text{ of first type were tested}$
 $6100 - x = 2500 \text{ of second type were tested}$

29. Assume the customer is located between A and B at a distance x from A.
 $3.40 + 0.0002x = 3.20 + 0.0002(228 - x)$
 $x = 64 \text{ mi from A}$

- 30.** Let x = number of L of gasoline added

$$\frac{15}{16} = 93.75\% \text{ gasoline} \left\{ \begin{array}{c} x \\ \hline 100\% \text{ gasoline} \\ \hline 8-x \\ \hline 75\% \text{ gasoline} \end{array} \right\} 8.0 \text{L}$$

$$0.9375(8.0) = x + 0.75(8.0 - x) \text{ from which}$$

$$x = 6.0 \text{L of gasoline added}$$

- 31.** Let x = number of liters of pure antifreeze added

x = number of liters of 50% antifreeze drained

$$0.25(12 - x) + x = 0.50(12)$$

$$3.0 - 0.25x + x = 6.0$$

$$0.75x = 3.0$$

$$x = 4.0 \text{ L}$$

- 32.** Let x = number of lb of sand

$$25\% \text{ sand} \left\{ \begin{array}{c} 100\% x \text{ sand} \\ \hline 250 - x \\ \hline 22\% \text{ sand} \end{array} \right\} 250 \text{ lbs}$$

$$0.25(250) = x + 0.22(250 - x) \text{ from which}$$

$$x = 9.6 \text{ lbs of sand}$$

- 33.** v = speed of car when it overtakes semitrailer

v = speed of car as it passes semitrailer

In passing, 25 m are covered in 10 s at a relative speed of $v - 70$. Changing 25 m to kilometers,

10 s to hours, and using $d = rt$ gives

$$\frac{25}{1000} = (v - 70) \left(\frac{10}{3600} \right) \text{ from which}$$

$$v = \frac{25(3600)}{1000(10)} + 70$$

$$v = 79 \text{ km/h}$$

- 34.** t = time for primary wave to reach station

$t + 2$ = time for secondary wave to reach station

$$8.0t = 5.0(t + 2) \text{ from which}$$

$$t = \frac{10}{3.0} \text{ min}$$

$$\text{distance} = 8.0t = 8.0 \cdot \frac{10}{3.0} \left(\frac{60 \text{ s}}{\text{min}} \right) = 1600 \text{ km}$$

Chapter 1 Review Exercises

1. $(-2) + (-5) - 3 = -7 - 3 = -10$

2. $6 - 8 - (-4) = -2 + 4 = 2$

3. $\frac{(-5)(6)(-4)}{(-2)(3)} = \frac{(-30)(-4)}{-6} = \frac{120}{-6} = -20$

4. $\frac{(-9)(-12)(-4)}{24} = \frac{108(-4)}{24} = \frac{-432}{24} = -18$

5. $-5 - |2(-6)| + \frac{-15}{3} = -5 - |-12| + (-5)$
 $= -5 - 12 - 5$
 $= -17 - 5$
 $= -22$

6. $3 - 5| -3 - 2| - \frac{| -4 |}{-4} = 3 - 5| -5 | - \frac{4}{-4}$
 $= 3 - 5(5) + 1$
 $= 3 - 25 + 1$
 $= -21$

7. $\frac{18}{3-5} - (-4)^2 = \frac{18}{-2} - 16 = -9 - 16 = -25$

8. $-3(-3)^2 - \frac{-8}{(-2) - |-4|} = -9 - \frac{-8}{-2 - 4} = -9 - \frac{-8}{-6}$
 $= -9 - \frac{4}{3} = -\frac{31}{3}$

9. $\sqrt{16} - \sqrt{64} = 4 - 8 = -4$

10. $-\sqrt{81+144} = -\sqrt{225} = -15$

11. $(\sqrt{7})^2 - \sqrt[3]{8} = 7 - 2 = 5$

12. $-\sqrt[4]{16} + (\sqrt{6})^2 = -2 + 6 = 4$

13. $(-2rt^2)^2 = 4r^2(t^2)^2 = 4r^2t^4$

14. $(3a^0b^{-2})^3 = (3b^{-2})^3 = 3^3(b^{-2})^3 = 27b^{-6} = \frac{27}{b^6}$

15. $-3mn^{-5}t(8m^{-3}n^4) = -24m^{1-3}n^{-5+4}t = -24m^{-2}n^{-1}t$
 $= -\frac{24t}{m^2n}$

16. $\frac{15p^4q^2r}{5pq^5r} = \frac{3p^3}{q^3}$

17. $\frac{-16N^{-2}(NT^2)}{-2N^0T^{-1}} = 8N^{-2+1}T^{2-(-1)}$
 $= 8N^{-1}T^3$
 $= \frac{8T^3}{N}$

18. $\frac{-35x^{-1}y(x^2y)}{5xy^{-1}} = \frac{-7y^2(x^2y)}{x^2} = -7y^3$

19. $\sqrt{45} = \sqrt{9 \cdot 5} = 3\sqrt{5}$

20. $\sqrt{9+36} = \sqrt{45} = 3\sqrt{5}$

21. (a) 8000 has 1 significant digits

(b) 8000 rounded to 2 significant digits is 8000

22. (a) 21,490 has 4 significant digits

(b) 21,490 rounded to 2 significant digits is 21,000

23. (a) 9.050 has 4 significant digits

(b) 9.050 rounded to 2 significant digits is 9.1

24. (a) 0.7000 has 4 significant digits

(b) 0.7000 rounded to 2 significant digits is 0.70

25. $37.3 - 16.92(1.067)^2 = 18.03676612$

on a calculator; 18.0

26. $\frac{8.896 \times 10^{-12}}{-3.5954 + 6.0449} = 3.63176158 \times 10^{-12}$, calculator

$= 3.632 \times 10^{-12}$, 4 significant digits

27. $\frac{\sqrt{0.1958+2.844}}{3.142(65)^2} = 1.313377619 \times 10^{-4}$, calculator
 $= 1.3 \times 10^{-4}$, 2 significant digits

28. $\frac{1}{0.03568} + \frac{37.466}{(29.63)^2} = 70.70195457$, calculator
 $= 70.70$, 4 significant digits

29. $a - 3ab - 2a + ab = a - 2a - 3ab + ab = -a - 2ab$

30. $xy - y - 5y - 4xy = xy - 4xy - 6y = -3xy - 6y$

31. $6LC - (3 - LC) = 6LC - 3 + LG = 7LC - 3$

32. $-(2x - b) - 3(-x - 5b) = -2x + b + 3x + 15b$
 $= x + 16b$

33. $(2x - 1)(5 + x) = 2x^2 + 10x - x - 5$
 $= 2x^2 + 9x - 5$

34. $(C - 4D)(D - 2C) = CD - 2C^2 - 4D^2 + 8CD$
 $= -2C^2 + 9CD - 4D^2$

35. $(x + 8)^2 = (x + 8)(x + 8) = x^2 + 8x + 8x + 64$
 $= x^2 + 16x + 64$

36. $(2r - 9s)^2$
 $= (2r - 9s)(2r - 9s) = 4r^2 - 9rs - 9rs + 81s^2$
 $= 4r^2 - 18rs + 81s^2$

37. $\frac{2h^3k^2 - 6h^4k^5}{2h^2k} = \frac{2h^3k^2}{2h^2k} - \frac{6h^4k^5}{2h^2k}$
 $= hk - 3h^2k^4$

38. $\frac{4a^2x^3 - 8ax^4}{-2ax^2} = \frac{4a^2x^3}{-2ax^2} - \frac{8ax^4}{-2ax^2} = -2ax + 4x^2$

39. $4R - [2r - (3R - 4r)] = 4R - [2r - 3R + 4r]$
 $= 4R - [6r - 3R]$
 $= 4R - 6r + 3R$
 $= 7R - 6r$

40. $-3b - [3a - (a - 3b)] + 4a = -3b - [3a - a + 3b] + 4a$
 $= -3b - [2a + 3b] + 4a$
 $= -3b - 2a - 3b + 4a$
 $= 2a - 5b$

41. $2xy - \{3z - [5xy - (7z - 6xy)]\}$
 $= 2xy - \{3z - [5xy - 7z + 6xy]\}$
 $= 2xy - \{3z - [11xy - 7z]\}$
 $= 2xy - \{3z - 11xy + 7z\}$
 $= 2xy - \{10 - 11xy\}$
 $= 2xy - 10z + 11xy$
 $= 13xy - 10z$

42. $x^2 + 3b + [(b - y) - 3(2b - y + z)]$
 $= x^2 + 3b + [b - y - 6b + 3y - 3z]$
 $= x^2 + 3b + [-5b + 2y - 3z]$
 $= x^2 - 2b + 2y - 3z$

43. $(2x + 1)(x^2 - x - 3) = 2x^3 - 2x^2 - 6x + x^2 - x - 3$
 $= 2x^3 - x^2 - 7x - 3$

44. $(x - 3)(2x^2 + 1 - 3x) = 2x^3 - 3x^2 + x - 6x^2 + 9x - 3$
 $= 2x^3 - 9x^2 + 10x - 3$

45. $-3y(x - 4y)^2 = -3y(x^2 - 8xy + 16y^2)$
 $= -3x^2y + 24xy^2 - 48y^3$

46. $-s(4s - 3t)^2 = -s(16s^2 - 24st + 9t^2)$

47. $3p[(q - p) - 2p(1 - 3q)] = 3p[q - p - 2p + 6pq]$
 $= 3p[q - 3p + 6pq]$
 $= 3pq - 9p^2 + 18p^2q$

48. $3x[2y - r - 4(x - 2r)] = 3x[2y - r - 4x + 8r]$
 $= 3x[2y + 7r - 4x]$
 $= 6xy + 21xr - 12x^2$

$$\begin{aligned} \text{49. } \frac{12p^3q^2 - 4p^4q + 6pq^5}{2p^4q} &= \frac{12p^3q^2}{2p^4q} - \frac{4p^4q}{2p^4q} + \frac{6pq^5}{2p^4q} \\ &= \frac{6q}{p} - 2 + \frac{3q^4}{p^3} \end{aligned}$$

$$\begin{aligned} \text{50. } \frac{27s^3t^2 - 18s^4t + 9s^2t}{-9s^2t} &= \frac{27s^3t^2}{-9s^2t} - \frac{18s^4t}{-9s^2t} + \frac{9s^2t}{-9s^2t} \\ &= -3st + 2s^2 - 1 \end{aligned}$$

$$\begin{aligned} \text{51. } x+6 \overline{)2x^2 + 7x - 30} &\quad 2x - 5 \\ &\underline{-2x^2 - 12x} \\ &\quad -5x - 30 \\ &\underline{-5x - 30} \end{aligned}$$

$$\begin{aligned} \text{52. } 2x+7 \overline{)4x^2 + 0x - 41} &\quad 2x - 7 \\ &\underline{-2x^2 - 14x} \\ &\quad -14x - 41 \\ &\underline{-14x - 49} \\ &\quad 8 \end{aligned}$$

$$\begin{aligned} \text{53. } 3x-1 \overline{)3x^3 - 7x^2 + 11x - 3} &\quad x^2 - 2x + 3 \\ &\underline{-3x^3 + x^2} \\ &\quad -6x^2 + 11x \\ &\underline{-6x^2 + 2x} \\ &\quad 9x - 3 \\ &\underline{9x - 3} \end{aligned}$$

$$\begin{aligned} \text{54. } w-3 \overline{)w^3 - 4w^2 + 7w - 12} &\quad w^2 - w + 4 \\ &\underline{-w^3 + 3w^2} \\ &\quad -w^2 + 7w \\ &\underline{-w^2 + 3w} \\ &\quad 4w - 12 \\ &\underline{4w - 12} \end{aligned}$$

$$\begin{aligned} \text{55. } x+3 \overline{)4x^4 + 10x^3 + 0x^2 + 18x - 1} &\quad 4x^3 - 2x^2 + 6x \\ &\underline{-4x^4 - 12x^3} \\ &\quad -2x^3 + 0x^2 \\ &\underline{-2x^3 - 6x^2} \\ &\quad 6x^2 + 18x \\ &\underline{6x^2 + 18x} \\ &\quad -1 \end{aligned}$$

$$\begin{aligned} \text{56. } 2x+3 \overline{)8x^3 + 0x^2 - 14x + 3} &\quad 4x^2 - 6x + 2 \\ &\underline{-8x^3 - 12x^2} \\ &\quad -12x^2 - 14x \\ &\underline{-12x^2 - 18x} \\ &\quad 4x + 3 \\ &\underline{4x + 6} \\ &\quad -3 \end{aligned}$$

$$\begin{aligned} \text{57. } -3\{(r+s-t) - 2[(3r-2s)-(t-2s)]\} &= -3\{(r+s-t) - 2[3r-2s-t+2s]\} \\ &= -3\{r+s-t-2[3r-t]\} \\ &= -3\{r+s-t-6r+2t\} \\ &= -3\{-5r+s+t\} \\ &= 15r-3s-3t \end{aligned}$$

$$\begin{aligned} \text{58. } (1-2x)(x-3) - (x+4)(4-3x) &= x-3-2x^2+6x-4x+3x^2-16+12x \\ &= x^2+15x-19 \end{aligned}$$

$$\begin{aligned} \text{59. } 2y-1 \overline{)2y^3 + 9y^2 - 7y + 5} &\quad y^2 + 5y - 1 \\ &\underline{-2y^3 - y^2} \\ &\quad 10y^2 - 7y \\ &\underline{10y^2 - 5y} \\ &\quad -2y + 5 \\ &\underline{-2y + 1} \\ &\quad 4 \end{aligned}$$

$$\begin{array}{r} 3x+4y \\ \hline 2x-y \sqrt{6x^2+5xy-4y^2} \\ \underline{6x^2-3xy} \\ 8xy-4y^2 \\ \underline{8xy-4y^2} \end{array}$$

$$\begin{aligned} 61. \quad 3x+1 &= x-8 \\ 3x-x &= -8-1 \\ 2x &= -9 \\ x &= \frac{-9}{2} \end{aligned}$$

$$\begin{aligned} 62. \quad 4y-3 &= 5y+7 \\ -3-7 &= 5y-4y \\ y &= -10 \end{aligned}$$

$$\begin{aligned} 63. \quad \frac{5x}{7} &= \frac{3}{2} \\ 2(5x) &= 3(7) \\ 10x &= 21 \\ x &= \frac{21}{10} \end{aligned}$$

$$\begin{aligned} 64. \quad \frac{2(4-N)}{-3} &= \frac{5}{4} \\ 8(4-N) &= -15 \\ 32-8N &= -15 \\ 8N &= -47 \\ N &= \frac{-47}{8} \end{aligned}$$

$$\begin{aligned} 65. \quad -6x+5 &= -3(x-4) \\ -6x+5 &= -3x+12 \\ 3x &= -7 \\ x &= \frac{-7}{3} \\ 66. \quad -2(-4-y) &= 3y \\ 8+26 &= 3y \\ y &= 8 \end{aligned}$$

$$\begin{aligned} 67. \quad 2s+4(3-s) &= 6 \\ 2s+12-4s &= 6 \\ -2s &= -6 \\ s &= 3 \end{aligned}$$

$$\begin{aligned} 68. \quad 2|x|-1 &= 3 \\ 2|x| &= 4 \\ |x| &= 2 \\ x &= \pm 2 \end{aligned}$$

$$\begin{aligned} 69. \quad 3t-2(7-t) &= 5(2t+1) \\ 3t-14+2t &= 10t+5 \\ 5t-14 &= 10t+5 \\ -5t &= 19 \\ t &= \frac{-19}{5} \end{aligned}$$

$$\begin{aligned} 70. \quad -(8-x) &= x-2(2-x) \\ -8+x &= x-4+2x \\ 2x &= -4 \\ x &= -2 \end{aligned}$$

$$\begin{aligned} 71. \quad 2.7+2.0(2.1x-3.4) &= 0.1 \\ 2.7+2.0(2.1x)-2.0(3.4) &= 0.1 \\ 2.0(2.1x) &= 0.1-2.7+2.0(3.4) \\ x &= \frac{0.1-2.7+2.0(3.4)}{2.0(2.1)} \\ x &= 1, \text{ calculator} \\ x &= 1.0, 2 \text{ significant digits} \end{aligned}$$

$$\begin{aligned} 72. \quad 0.250(6.721-2.44x) &= 2.08 \\ 0.250(6.721)-0.250(2.44x) &= 2.08 \\ 0.250(2.44x) &= 2.08-(0.250)(6.721) \\ x &= \frac{2.08-0.250(6.721)}{0.250(2.44)} \\ x &= 0.6553278689, \text{ calculator} \\ x &= 0.655, 3 \text{ significant digits} \end{aligned}$$

$$73. \quad 60,000,000,000,000 = 6 \times 10^{13} \text{ bytes}$$

$$74. \quad 25,000 \text{ mi/h} = 2.5 \times 10^4 \text{ mi/h}$$

75. $192,000,000 \text{ km} = 1.92 \times 10^8 \text{ km}$

76. $1.02 \times 10^9 \text{ Hz} = 1,020,000,000 \text{ Hz}$

77. $2.53 \times 10^{13} \text{ mi} = 25,300,000,000,000 \text{ mi}$

78. $10^7 \text{ ft}^2 = 10,000,000 \text{ ft}^2$

79. $10^{-12} \text{ W/m}^2 = 0.000000000001 \text{ W/m}^2$

80. $0.00000015 \text{ m} = 1.5 \times 10^{-7} \text{ m}$

81. $1.5 \times 10^{-1} \text{ Bq/L} = 0.15 \text{ Bq/L}$

82. $0.00000018 \text{ m} = 1.8 \times 10^{-7} \text{ m}$

83. $V = \pi r^2 L$

$$L = \frac{V}{\pi r^2}$$

84. $R = \frac{2GM}{c^2} \Rightarrow 2GM = Rc^2 \Rightarrow G = \frac{Rc^2}{2M}$

85. $P = \frac{\pi^2 EI}{L^2}$

$$E = \frac{PL^2}{\pi^2 I}$$

86. $f = p(c-1) - c(p-1)$

$$f = pc - p - pc + c$$

$$p = c - f$$

87. $Pp + Qq = Rr$

$$Qq = Rr - Pp$$

$$q = \frac{Rr - Pp}{Q}$$

88. $V = IR + Ir \Rightarrow Ir = V - IR$

$$r = \frac{V - IR}{I}$$

89. $d = (n-1)A$

$$d = nA - A$$

$$na = d + A$$

$$n = \frac{d + A}{A}$$

90. $mu = (m+M)v \Rightarrow m+M = \frac{mu}{v} \Rightarrow M = \frac{mu}{v} - m$

91. $N_1 = T(N_2 - N_3) + N_3 = TN_2 - TN_3 + N_3$

$$TN_2 = N_1 + TN_3 - N_3$$

$$N_2 = \frac{N_1 + TN_3 - N_3}{T}$$

92. $Q = \frac{kAt(T_2 - T_1)}{L}$

$$QL = kAt(T_2 - T_1)$$

$$\frac{QL}{kAt} = T_2 - T_1$$

$$T_1 = T_2 - \frac{QL}{kAt}$$

93. $R = \frac{A(T_2 - T_1)}{H}$

$$RH = AT_2 - AT_1$$

$$AT_2 = RH + AT_1$$

$$T_2 = \frac{RH + AT_1}{A}$$

94. $Z^2 \left(1 - \frac{\lambda}{2a}\right) = k$

$$1 - \frac{\lambda}{2a} = \frac{k}{z^2}$$

$$\frac{\lambda}{2a} = 1 - \frac{k}{z^2}$$

$$\lambda = 2a \left(1 - \frac{k}{z^2}\right)$$

95. $d = kx^2 [3(a+b) - x] = kx^2 [3a + 3b - x]$

$$3a + 3b - x = \frac{d}{kx^2} \Rightarrow 3a = \frac{d}{kx^2} + x - 3b$$

$$a = \frac{d}{3kx^2} + \frac{x}{3} - b$$

96. $V = V_o [1 + 3a(T_2 - T_1)] \Rightarrow \frac{V}{V_o} = 1 + 3aT_2 - 3aT_1$

$$3aT_2 = \frac{V}{V_o} - 1 + 3aT_1$$

$$T_2 = \frac{V}{3aV_o} - \frac{1}{3a} + T_1$$

97. $\frac{5.25 \times 10^{13}}{6.4 \times 10^4} = 8.2 \times 10^8$

98. $t = 0.25\sqrt{h} = 0.25\sqrt{66} = 2.03s$

99. $0.553 \text{ km} = 553 \text{ m}; 553 \text{ m} - 442 \text{ m} = 111 \text{ m}$

100. $t = \left(\frac{n}{2650} \right)^2 = \left(\frac{4.8 \times 10^3}{2650} \right)^2 = 3.28s$

101. $\frac{R_1 R_2}{R_1 + R_2} = \frac{0.0275(0.0590)}{0.0275 + 0.0590} = 0.0188 \Omega$

102. $d = 1.5 \times 10^{11} \sqrt{\frac{m}{M}} = 1.5 \times 10^{11} \sqrt{\frac{5.98 \times 10^{24}}{1.99 \times 10^{30}}} \\ d = 2.6 \times 10^8 \text{ m}$

103. $(x - 2a) + 3(x + 2a) = x - 2a + 3x + 6a \\ = 4x + 4a \text{ ft}$

104. $(Ai - R)(1+i)^2 = (Ai - R)(1+2i+i^2) \\ = Ai + 2Ai^2 + Ai^3 - R - 2Ri - Ri^2$

105. $4(t+h) - 2(t+h)^2 = 4t + 4h - 2(t^2 + 2th + h^2) \\ = 4t + 4h - 2t^2 - 4th - 2h^2$

106. $\frac{k^2 r - 2h^2 k + h^2 r v^2}{k^2 r} = 1 - \frac{2h^2}{kr} + \frac{h^2 v^2}{k^2}$

107. $3 \times 18 \div (9 - 6) = 3 \times 18 \div 3 = 54 \div 3 = 18$

$3 \times 18 \div 9 - 6 = 54 \div 9 - 6 = 6 - 6 = 0$,
yes, the value changes

108. $(3 \times 18) \div 9 - 6 = 54 \div 9 - 6 = 6 - 6 = 0$

$3 \times 18 \div 9 - 6 = 54 \div 9 - 6 = 6 - 6 = 0$,
no, the value does not change

109. $x - (3 - x) = 2x - 3$

$$x - 3 + x = 2x - 3$$

$2x - 3 = 2x - 3$, the equation is an identity

110. $7 - (2 - x) = x + 2$

$$7 - 2 + x = x + 2$$

$5 = 2$, contradiction

111. $x = 2, y = -4$

$$\begin{aligned} (a) \quad 2|x| - 2|y| &= 2|2| - 2|-4| \\ &= 2(2) - 2(4) \\ &= -4 \end{aligned}$$

$$\begin{aligned} (b) \quad 2|x - y| &= 2|2 - (-4)| \\ &= 2|2 + 4| \\ &= 2|6| + 2(6) \\ &= 12 \end{aligned}$$

112. If $a < 0$, $|a| = -a$.

113. $|3 - x| + 7 = 2x$

$$|3 - x| = 2x - 7$$

$$3 - x = 2x - 7 \text{ or } 3 - x = -(2x - 7)$$

$$3x = 10 \text{ or } 3 - x = -2x + 7$$

$$x = \frac{10}{3} \text{ or } x = 4$$

$$x = \frac{10}{3} \text{ does not check}$$

$$3 - x = 3 - 4 = -1 < 0 \text{ and}$$

$$x = 4 \text{ checks}$$

$$x = 4 \text{ is the solution}$$

114. $|x - 4| + 6 = 3x$

$$|x - 4| = 3x - 6$$

$$x - 4 = 3x - 6 \quad \text{or} \quad x - 4 = -(3x - 6)$$

$$2 = 2x \quad x - 4 = -3x + 6$$

$$x = 1 \quad 4x = 10$$

$$x = \frac{5}{2}$$

$x = 1$ does not check

$$x = \frac{5}{2} \text{ is the solution}$$

$$\begin{aligned}
 115. \quad (x-y)^3 &= (x-y)(x-y)(x-y) \\
 &= (-\cancel{(y-x)})(-\cancel{(y-x)})(-\cancel{(y-x)}) \\
 &= -(\cancel{y-x})(\cancel{y-x})(\cancel{y-x}) \\
 &= -(\cancel{y-x})^3
 \end{aligned}$$

116. No division is not associative as the counterexample shows.

$$(8 \div 4) \div 2 = 2 \div 2 = 1$$

$$8 \div (4 \div 2) = 8 \div 2 = 4$$

$$117. \quad \frac{8 \times 10^{-3}}{2 \times 10^4} = 4 \times 10^{-7}$$

$$118. \quad \frac{\sqrt{4+36}}{\sqrt{4}} = \frac{\sqrt{40}}{\sqrt{4}} = \frac{\sqrt{4(10)}}{2} = \frac{\sqrt{10}}{2} = \sqrt{10}$$

$$\begin{aligned}
 119. \quad 250 \text{ hp} &= 250 \text{ hp} \left(\frac{746.0 \text{ W}}{\text{hp}} \right) \left(\frac{\text{kW}}{1000 \text{ W}} \right) \\
 &= 190 \text{ kW}
 \end{aligned}$$

$$\begin{aligned}
 120. \quad 32 \frac{\text{lb}}{\text{in.}^2} &= 32 \frac{\text{lb}}{\text{in.}^2} \cdot \frac{4.448 \text{ N}}{\text{lb}} \cdot \frac{1 \text{ in.}^2}{2.54^2 \text{ cm}^2} \cdot \frac{100^2 \text{ cm}^2}{\text{m}^2} \\
 &= 220,000 \text{ N/m}^2
 \end{aligned}$$

$$\begin{aligned}
 121. \quad x + x + 72 &= 190 \Rightarrow 2x = 118 \Rightarrow x = \$59 \\
 &\quad x + 72 = \$131
 \end{aligned}$$

$$\begin{aligned}
 122. \quad x + x + 1100 &= 9500 \Rightarrow 2x = 8400 \Rightarrow x = \$4200 \\
 &\quad x + 1100 = \$5300
 \end{aligned}$$

$$123. \quad x + y + z = 560$$

$$x = 2y$$

$$z = 2x$$

from which

$$x = 160 \text{ cm}^3, y = 80 \text{ cm}^3, z = 320 \text{ cm}^3$$

$$124. \quad (5.5-w)(8.0) = (5.5+w)(5.0)$$

$$44 - 8.0w = 5.5(5.0) + 5.0w$$

$$w = \frac{44 - 5.5(5.0)}{5.0 + 8.0}$$

$$= 1.269230769, \text{ calculator}$$

$$w = 1.3 \text{ mi/h}$$

$$\begin{aligned}
 125. \quad 2.4 \times 10^{-6}R + 2.4 \times 10^{-6}(R + 1200) &= 12.0 \times 10^{-3} \\
 4.86 \times 10^{-6}R &= 12.0 \times 10^{-3} - 1200 \times 2.4 \times 10^{-6} \\
 R &= 1900 \Omega \\
 R + 1200 &= 3100 \Omega
 \end{aligned}$$

$$126. \quad x + 4x = 4.0 \Rightarrow 5x = 4.0$$

$$x = 0.80 \text{ ppm}$$

$$4x = 3.2 \text{ ppm}$$

$$\begin{aligned}
 127. \quad \frac{12 \text{ h}}{450 \text{ m}} &= \frac{x}{250 \text{ m}} \\
 x &= 6.7 \text{ h}
 \end{aligned}$$

$$\begin{aligned}
 128. \quad 15G + G &= 6.6 \Rightarrow G = \frac{6.6}{16} = 0.4125, \text{ calculator} \\
 15g &= 6.1875, \text{ calculator} \\
 \text{mixture contains } 6.2\text{L oil and } 0.41\text{L gasoline}
 \end{aligned}$$

$$\begin{aligned}
 129. \quad 17.4(t+2) + 21.8t &= 634 \Rightarrow t = \frac{634 - 34.8}{39.2} \\
 &= 15.28571429, \\
 &\quad \text{calculator}
 \end{aligned}$$

Ships pass 15.3 h after the second ship starts.

$$130. \quad \text{distance pond to fire} = \text{distance fire to pond}$$

$$70t = 105 \left(\frac{1}{2} - t \right)$$

$$t = 0.3 \text{ h} = 18 \text{ min}$$

$$131. \quad x + y = 1000$$

$$0.0050x + 0.0075y = 0.0065(1000)$$

$$\text{from which} \quad x = 400 \text{ L}$$

$$y = 600 \text{ L}$$

$$132. \quad x + y = 18,000 \Rightarrow y = 18,000 - x$$

$$72x + 150y = 120(18,000)$$

$$72x + 150(18,000 - x) = 120(18,000)$$

$$x = \frac{90,000}{13} = 6923$$

$$y = 18,000 - x = \frac{144,000}{13} = 11,077$$

6923 Mg of 72 L/Mg rock are needed

11,077 Mg of 150 L/Mg rock are needed

133. $\frac{\text{square ft of tile}}{\text{square ft in house}} = 0.25$

$$\frac{0.15(2200)}{2200 + x} = 0.25$$

$x = 290 \text{ ft}^2$ in kitchen and entry

134. $x + y = 200 \Rightarrow y = 200 - x$

$$\frac{9}{24}x + \frac{18}{24}y = \frac{14}{24}(200) \Rightarrow 9x + 18y = 2800$$

$$9x + 18(200 - x) = 2800$$

$$x = 89 \Rightarrow y = 111$$

89gm of 9-karat gold mised with 111 gm of
18-karat gold will produce a mixture of 200 gm
of 14-karat gold.

135. $P = P_0 + P_0 rt$

$$P_0 rt = P - P_0$$

$$r = \frac{P - P_0}{P_0 t}$$

$$r = \frac{7625 - 6250}{6250(4.000)} = 0.055$$

$$r = 5.5\%$$

On a calculator $r = (7625 - 6250) / (6250(4.000))$.